

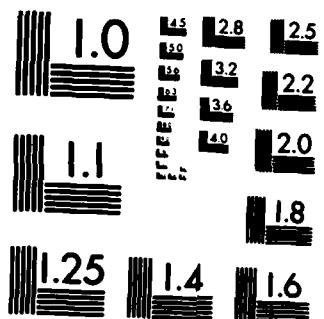
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(ARS-50) DESIGN REPRESENT.. (U) DAVID W TAYLOR NAVAL  
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# DAVID W. TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER

DTNSRDC/SPD-0957-03



Bethesda, Maryland 20084

ANALYSIS OF WAKE SURVEY DATA FOR A  
SALVAGE SHIP (ARS-50) DESIGN  
REPRESENTED BY MODEL 5391  
WITH KORT NOZZLE

AD A125043

By

David M. Rawson

and

E. E. West

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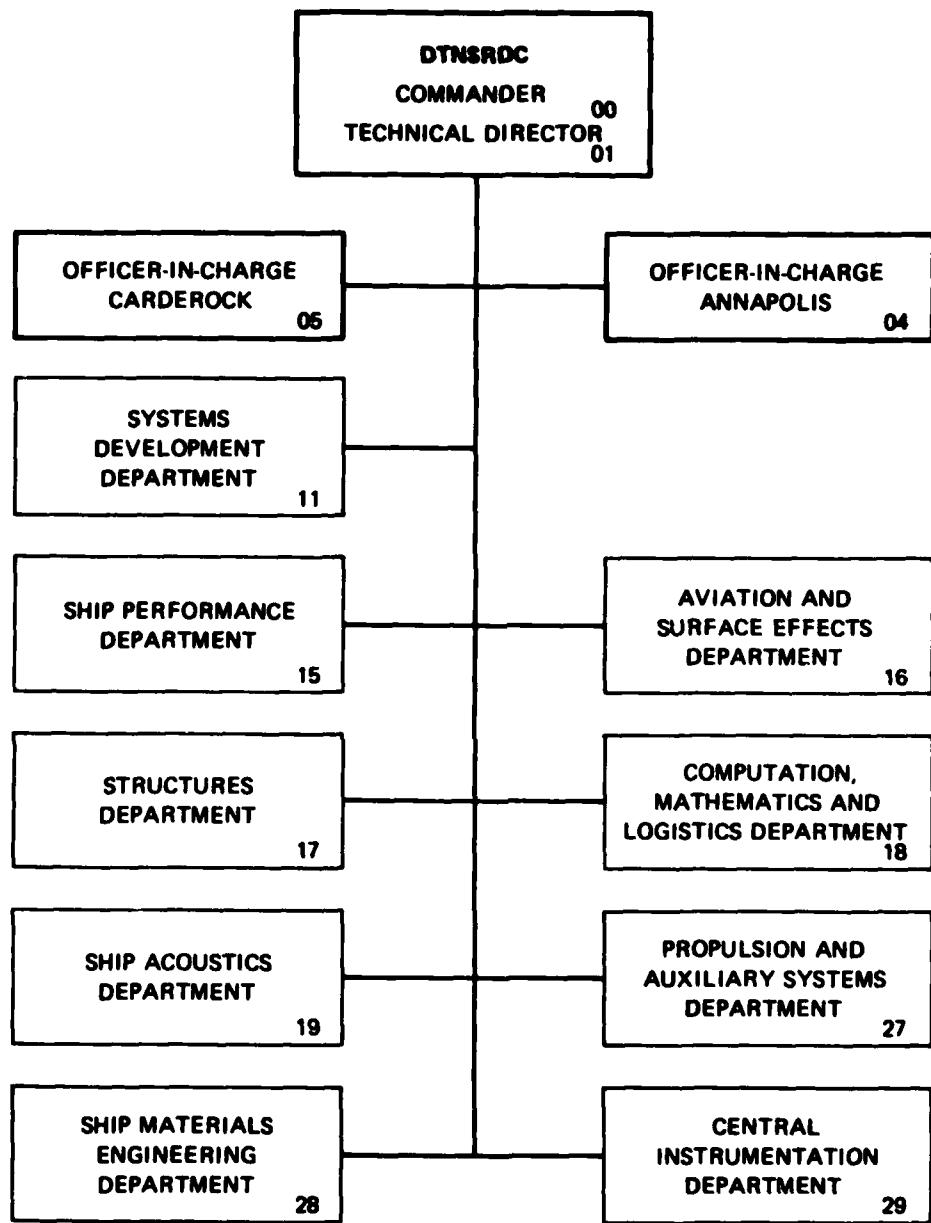
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February 1983

DTNSRDC/SPD-0957-03

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## MAJOR DTNSRDC ORGANIZATIONAL COMPONENTS



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SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

REPORT DOCUMENTATION PAGE		READ INSTRUCTIONS BEFORE COMPLETING FORM
1. REPORT NUMBER  DTNSRDC/SPD-0957-03	2. GOVT ACCESSION NO.  <i>A125-043</i>	3. RECIPIENT'S CATALOG NUMBER
4. TITLE (and Subtitle)  ANALYSIS OF WAKE SURVEY DATA FOR A SALVAGE SHIP (ARS-50) DESIGN REPRESENTED BY MODEL 5391 WITH KORT NOZZLE	5. TYPE OF REPORT & PERIOD COVERED  FINAL	
7. AUTHOR(s)  David M. Rawson E. E. West	8. CONTRACT OR GRANT NUMBER(s)	
9. PERFORMING ORGANIZATION NAME AND ADDRESS  David W. Taylor Naval Ship R&D Center Ship Performance Department Bethesda, Maryland 20084	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS  NAVSEA Work Request N00024-82 DTNSRDC Work Unit 1521-730	
11. CONTROLLING OFFICE NAME AND ADDRESS  Naval Sea Systems Command Washington, D.C. 20362	12. REPORT DATE  February 1983	
14. MONITORING AGENCY NAME & ADDRESS// different from Controlling Office)	13. NUMBER OF PAGES  47	
15. SECURITY CLASS. (of this report)  Unclassified		
15a. DECLASSIFICATION/DOWNGRADING SCHEDULE		
16. DISTRIBUTION STATEMENT (of this Report)  Approved for Public Release: Distribution Unlimited		
17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)		
18. SUPPLEMENTARY NOTES		
19. KEY WORDS (Continue on reverse side if necessary and identify by block number)  Salvage Ship    Kort Nozzle Wake Survey Pitot Tube Rake Model Experiments		
20. ABSTRACT (Continue on reverse side if necessary and identify by block number)  A wake survey was conducted to aid in the design of a kort nozzle propeller for a salvage ship (ARS-50) represented by DTNSRDC Model 5391-1 (Hydraulics Model 7925-4). Pressure measurements were made with a rake of five-hole pitot tubes in order to obtain the flow velocity in the plane of the propeller. Several model configurations were tested in order to identify the effect of the nozzle on the flow and also the effect of a propeller installed just aft of the rake for the purpose of simulating a realistic flow		

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20. Abstract (continued)

through the nozzle. Harmonic analyses of the circumferential distribution of the velocity component ratios were performed on the model experimental data and the results are reported herein.

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Approved by:	<i>[Signature]</i>
Date:	1964
File No.:	100-10000
Classification:	Confidential
Control No.:	100-10000
Serial No.:	100-10000
Disposition:	Not Applicable
Availability Dates:	Not Applicable
Avail. and/or Special:	Special
Date:	1964

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NOTATION

<u>CONVENTIONAL SYMBOL</u>	<u>SYMBOL APPEARING ON PLOTS</u>	<u>DEFINITION</u>
$A_N$	COS COEF	The cosine coefficient of the $N^{\text{th}}$ harmonic*
$B_N$	SIN COEF	The sine coefficient of the $N^{\text{th}}$ harmonic*
D	---	Propeller diameter
$J_V$	---	Apparent advance coefficient $J_V = \frac{V}{nD}$ (dimensionless)
L	---	Length of ship (LBP)
N	N	Harmonic number
n	---	Propeller revolutions
r/R or x	Radius or RAD.	Distance (r) from the propeller axis expressed as a ratio of the propeller radius (R)
V	V	Actual model or ship velocity
$v_b(x, \theta)$	---	Resultant inflow velocity to blade for a given point
$\bar{v}_b(x)$	---	Mean resultant inflow velocity to blade for a given radius
$v_r(x, \theta)$	VR	Radial component of the fluid velocity for a given point (positive toward the shaft centerline)
$\bar{v}_r(x)$	---	Mean radial velocity component for a given radius
$v_r(x, \theta)/V$	VR/V	Radial velocity component ratio for a given point
$\bar{v}_r(x)/V$	VRBAR	Mean radial velocity component ratio for a given radius
$v_t(x, \theta)$	VT	Tangential component of the fluid velocity for a given point (positive in a counterclockwise direction looking forward)

\*See footnote on the following page

NOTATION (Continued)

$\bar{v}_t(x)$	---	Mean tangential velocity component for a given radius
$v_t(x, \theta)/v$	VT/V	Tangential velocity component ratio for a given point
$\bar{v}_t(x)/v$	VTBAR	Mean tangential velocity component ratio for a given radius
$(\tilde{v}_t(x)/v)_N$	AMPLITUDE	Amplitude ( $B_N$ for single screw symmetric; $C_N$ otherwise) of Nth harmonic of the tangential velocity component ratio for a given radius*
$v_x(x, \theta)$	VX	Longitudinal (normal to the plane of survey) component of the fluid velocity for a given point (positive in the astern direction)
$\bar{v}_x(x)$	---	Mean longitudinal velocity component for a given radius
$v_x(x, \theta)/v$	VX/V	Longitudinal velocity component ratio for a given point
$\bar{v}_x(x)/v$	VXBAR	Mean longitudinal velocity component ratio for a given radius
$(\tilde{v}_x(x)/v)_N$	AMPLITUDE	Amplitude ( $A_N$ for single screw symmetric; $C_N$ otherwise) of Nth harmonic of the longitudinal velocity component ratio for a given radius*
$\phi_N$	PHASE ANGLE	Phase Angle of Nth harmonic*

\*The harmonic amplitudes of any circumferential velocity distribution  $f(\theta)$  are the coefficients of the Fourier Series:

$$f(\theta) = A_0 + \sum_{N=1}^{\infty} A_N \cos(N\theta) + \sum_{N=1}^{\infty} B_N \sin(N\theta)$$

$$= A_0 + \sum_{N=1}^{\infty} C_N \sin(N\theta + \phi_N)$$

NOTATION (Continued)

$1-w(x)$

$1-WX$

Volumetric mean velocity ratio from the hub to a given radius

$$1-w(r/R) = \frac{\left[ 2 \cdot \int_{r_{\text{hub}}/R}^{r/R} (\bar{v}_{x_c}(x)/v) \cdot x \cdot dx \right]}{(r/R)^2 - (r_{\text{hub}}/R)^2}$$

$$\text{where } \bar{v}_{x_c}(x)/v = \int_0^{2\pi} \left[ \frac{v_{x_c}(x, \theta)}{2\pi v} \right] d\theta$$

$$\text{and } v_{x_c}(x, \theta)/v = (v_x(x, \theta)/v) - (v_t(x, \theta)/v) \tan(\beta(x, \theta))$$

$1-w_v(x)$

$1-WVX$

Volumetric mean velocity ratio from the hub to a given radius (without the tangential velocity correction)

$$1-w(r/R) = \frac{\left[ 2 \cdot \int_{r_{\text{hub}}/R}^{r/R} (\bar{v}_x(x)/v) \cdot x \cdot dx \right]}{(r/R)^2 - (r_{\text{hub}}/R)^2}$$

$x/L$

Distance from forward perpendicular expressed as a ratio of the overall length ( $L$ )

$\beta(x, \theta)$

---

Advance angle in degrees for a given point

$\bar{\beta}(x)$

BBAR

Mean advance angle in degrees for a given radius

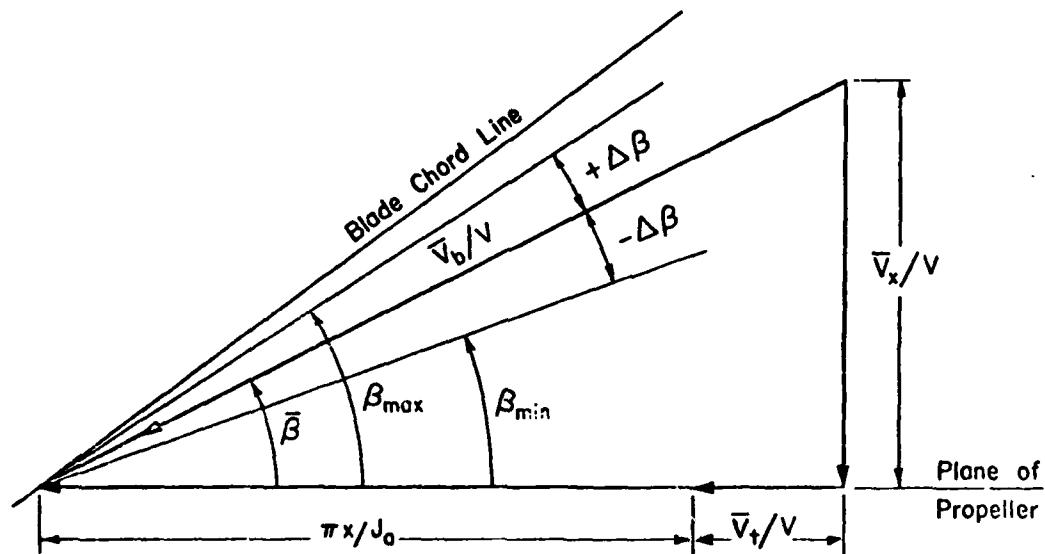
$+\Delta\beta$

BPOS

Variation of the maximum advance angle from the mean for a given radius

NOTATION (Continued)

$-\Delta\beta$	BNEG	Variation of the minimum advance angle from the mean for a given radius
$\theta$	Angle in Degrees	Position angle (angular coordinate) in degrees



VELOCITY DIAGRAM OF BETA ANGLES

### AMERICAN STANDARD AND METRIC EQUIVALENTS (U)

AMERICAN STANDARD	METRIC
1 inch	25.400 millimeter [0.0254 m (meter)]
1 foot	0.3048 m (meter)
1 foot per second	0.3048 m/s (meter per second)
1 knot	0.5144 m/s (meter per second)
1 pound (force)	4.4480 N (newtons)
1 degree (angle)	0.01745 rad (radians)
1 horsepower	0.7457 kW (kilowatts)
1 long ton	1.016 tonnes, 1.016 metric tons, or 1016.0 kilograms
1 inch water (60 deg F)	248.8 pa (pascals)

The notations used in this document are consistent with the International Towing Tank Conference (ITTC) Standard Symbols.\*

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\*International Towing Tank Conference Standard Symbols 1976, The British Ship Research Association, BSRA Technical Memorandum No. 500 (May 1976)

## ABSTRACT

A wake survey was conducted to aid in the design of a kort nozzle propeller for a salvage ship (ARS-50) represented by DTNSRDC Model 5391-1 (Hydronautics Model 7925-4). Pressure measurements were made with a rake of five-hole pitot tubes in order to obtain the flow velocity in the plane of the propeller. Several model configurations were tested in order to identify the effect of the nozzle on the flow and also the effect of a propeller installed just aft of the rake for the purpose of simulating a realistic flow through the nozzle. Harmonic analyses of the circumferential distribution of the velocity component ratios were performed on the model experimental data and the results are reported herein.

## ADMINISTRATIVE INFORMATION

The work was authorized by the Naval Sea Systems Command (NAVSEA) in accordance with Work Request Number N00024-82. The DTNSRDC Work Unit Number was 1521-730.

## INTRODUCTION

The Naval Sea Systems Command (NAVSEA) initiated a model experimental program at the David W. Taylor Naval Ship R&D Center (DTNSRDC) to aid in the calculation of alternating forces and moments of the ARS-50 salvage ship propeller. In this program, the Center was requested to perform wake surveys in the propeller plane of the ARS-50 Model with the kort nozzles. One survey was to be conducted while a propeller was operating to induce flow through the nozzle. A second survey was to be performed with the propeller removed. An additional wake survey was performed without the nozzle or propeller.

A powering investigation as well as a wake survey had been carried out by Anderson and Day<sup>1</sup> with the model of the ARS 50 fitted with an unshrouded propeller instead of the present kort nozzle propulsion system. The results of

---

<sup>1</sup> References are listed on page 7.

the wake survey with and without the kort nozzle and the harmonic analyses of the velocity components of the survey are presented herein.

#### DESCRIPTION OF MODEL

Model 5391, representing the 240 ft (73.1 m) ARS-50 salvage ship, was constructed of fiberglass by Hydronautics Inc. for experiments requested of them by NAVSEA. The linear ratio used was 15.357.

The appendages installed for the wake survey in addition to the kort nozzles included the shafts, struts, and bilge keels. A right angle drive was also installed to power the propeller (Hydronautics propeller 7925-2CD set at pitch-diameter ratio of 1.21) behind the kort nozzle. Photographs of the arrangement are shown in Figure 1. The appendage arrangement with the propeller removed for the wake survey without the induced flow through the kort nozzle is shown in Figure 2.

The wake surveys were conducted with the model ballasted to a draft representing 15.5 ft (4.7 m) even keel in the static condition. The model was then towed at a velocity representing a ship speed of 14.5 knots (7.5 m/s). Propeller revolutions representing 150 revolutions per minute (rpm) full-scale were set when the propeller was used.

A special wake survey rake was built with short pitot tubes so that the rake would be suitable for operation within the nozzle and have as small a clearance as possible from the operating propeller mounted just behind the rake. A drawing of the pitot tube rake arrangement is presented in Figure 3. The tubes were positioned radially at fractions of the propeller radius equalling 0.451, 0.591, 0.735, and 0.868, based on a 5.25 ft (1.6 m) propeller radius.

## PRESENTATION AND DISCUSSION OF RESULTS

This presentation is divided into three sections, the wake survey in the nozzle with the propeller induced flow, the survey in the nozzle without the propeller, and the survey without the nozzle or propeller. The advance angles were calculated using an advance coefficient,  $J_V$ , of 0.910.

### WITH PROPELLER

The circumferential distributions of the longitudinal, tangential, and radial velocity component ratios of the propeller induced flow are presented in graphical form in Figures 4 through 7. Tabulated values of the experimental velocity component ratios at the experimental radii are presented in Table 1. The radial distributions of the circumferential mean velocities and advance angles are plotted in Figures 8 and 9, respectively.

Harmonic analyses have been performed on the longitudinal and tangential velocity component ratios. The mean longitudinal ( $V_{XBAR}$ ), tangential ( $V_{TBAR}$ ), and radial ( $V_{RBAR}$ ) component ratios of the velocity vectors, and the volumetric mean wake velocity ratio ( $1-W_X$ ) are presented in Table 2 along with the calculated mean values of the advance angle ( $B_{BAR}$ ), and the maximum variations thereof, ( $B_{POS}$ ) and ( $B_{NEG}$ ). The amplitudes and phase angles for the four experimental and nine interpolated radii are tabulated for eight harmonics in Tables 3 and 4 for the longitudinal and tangential velocity components, respectively.

### WITHOUT PROPELLER

The circumferential distributions of the longitudinal, tangential, and radial velocity component ratios for the survey without the propeller are presented in graphical form in Figures 10 and 13. Tabulated values of the

experimental velocity component ratios at the experimental radii are presented in Table 5. The radial distributions of the circumferential mean velocities and advance angles are plotted in Figures 14 and 15, respectively and tabulated in Table 6. The amplitudes and phase angles from the harmonic analysis of the wake survey without the propeller are presented in Tables 7 and 8.

#### WITHOUT NOZZLE

The circumferential distributions of velocity component ratios for the survey without the nozzle or propeller are presented in graphical form in Figures 16 through 19. Tabulated values of the experimental velocity component ratios at the experimental radii are presented in Table 9. The radial distribution of the mean velocity component ratios and advance angles are plotted in Figures 20 and 21 respectively and tabulated in Table 10. This data was collected for comparison with reference 1. The amplitudes and phase angles from the harmonic analysis of the wake survey without the nozzle are presented in Tables 11 and 12.

In Figures 8, 9, 13, 14, 20, and 21, points marked by geometric symbols (triangle, square, etc.) represent actual measured data. The points marked by an "x" represent interpolations calculated by the computer.

The measurement system used in this velocity survey has been described by Grant and Lin<sup>2</sup>. The accuracy of the pressure transducer system is approximately plus or minus three hundredths of an inch of water pressure (7.5 pascal). The accuracy of the entire velocity survey apparatus is estimated to be  $\pm$  one percentage point on the longitudinal velocity component ratio, except in areas where steep velocity gradients occur. In these areas, such as behind a strut, the accuracy is significantly less.

Figure 22 presents a composite plot of the radial distribution of the mean longitudinal velocity component to illustrate the increase in flow velocity caused by the nozzle and propeller. The nozzle caused an increase in the axial flow through the propeller plane of approximately 6.5 percent while the propeller increased the flow through the nozzle by approximately 18.8 percent.

The tangential velocity component ratios were not affected appreciably by the flow velocity increase due to the nozzle or propeller.

The tangential velocity component ratios measured with the second and fourth pitot tubes ( $r/R$  values of 0.591 and 0.868) were considered to be too high and inaccurate. The observed inaccuracy was consistently present in all the experiments and was considered to be due to complications in the pitot tubes. This inaccuracy could best be seen in the angular location of the "cross-over" points. The cross-over point is the angular position at which the tangential velocity components are zero. The cross-over points are generally the same at all radii and they occurred at approximately  $150^\circ$  for the first and third pitot tubes ( $r/R = 0.451$  and  $0.735$ ) in these experiments and for all the experimental radii in reference 1. However, the cross-over points for  $V_T/V$  from the second and fourth tubes of the present experiments were at approximately  $120^\circ$ . To correct the tangential velocity values measured with tubes two and four, the data for each tube were reduced by a constant amount necessary to bring the value of  $V_T/V$  at  $150^\circ$  to zero.

A second harmonic analysis was performed with the adjusted tangential velocity component values. The adjustment had no effect on the longitudinal velocity components and the harmonic content of the wake was unchanged. Presented herein are the wake survey data as measured and the results of the

harmonic analyses of the measured data. The circumferential mean of the tangential velocity components are presented in Figures 8, 14, and 20 for both adjusted and unadjusted data.

#### CONCLUSIONS

A new pitot tube rake was constructed to allow measurements to be taken at the propeller plane inside the kort nozzle. The rake performed well, but there were inaccuracies in the tangential velocity component measurements from the second and fourth tubes. The inaccuracies did not effect the determination of the longitudinal velocities or the harmonic analysis of the wake.

The data for the ARS-50 wake survey appears reasonable. The results of the wake survey of the ARS-50 hull without a nozzle or propeller compare well, within acceptable limits, to the results obtained in a previous wake survey performed on the ARS-46. The installation of a kort nozzle in the propeller plane increases the axial flow through the propeller plane by 6.5 percent. The presence of a propeller rotating at 150 rpm, ship scale, will increase the flow through the nozzle by an additional 18.8 percent. The presence of the nozzle and rotating propeller did not appreciably change the tangential component of the wake.

#### REFERENCES

1. Anderson, K.J. and W.G. Day, "Predictions of Powering Performance Including Tow Rope Pull and the Results of Propeller Disk Wake Survey for the ARS-46 Salvage Ship Represented by Model 5391," DTNSRDC Report SPD-0957-01, (September 1980).
2. Grant, J.W. and A.C.M. Lin, "The Effects of Variations of Several Parameters on the Wake of the Propeller Plane for Series 60 - 0.60 C<sub>B</sub> Models," Appendices A and D, DTNSRDC Report 3024, pp. 105, (June 1969).



PSD 7449-6-82



PSD 7447-6-82



PSD 7445-6-82



PSD 7444-6-82

**Figure 1 - Photographs showing the ARS-50 Nozzle with Propeller  
and Wake Survey Pitot Tube Rake**



PSD 7480-7-82



PSD 7479-7-82



PSD 7481-7-82



PSD 7482-7-82

Figure 2 - Photographs showing the ARS-50 Nozzle with Wake Survey  
Pitot Rake but without Propeller

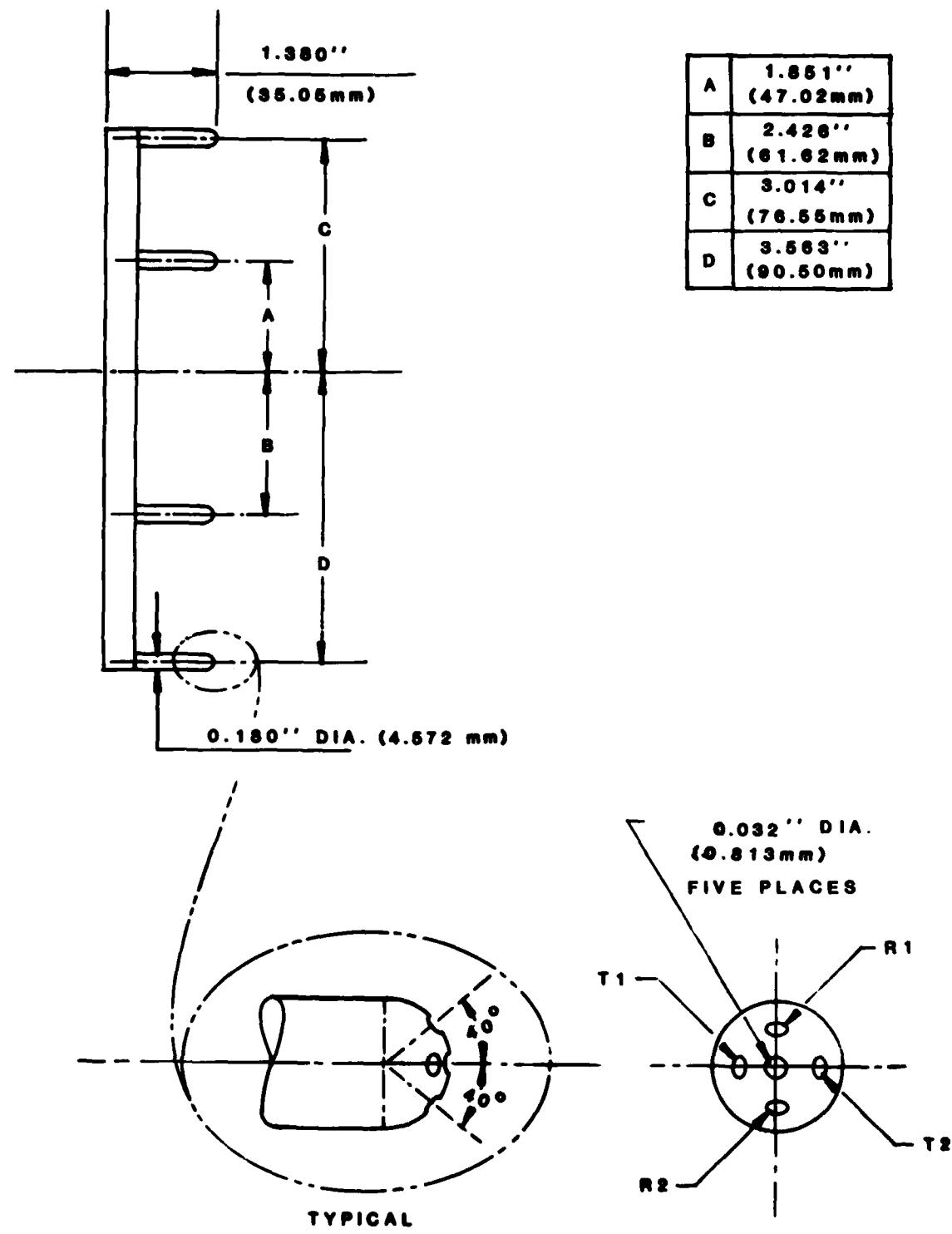
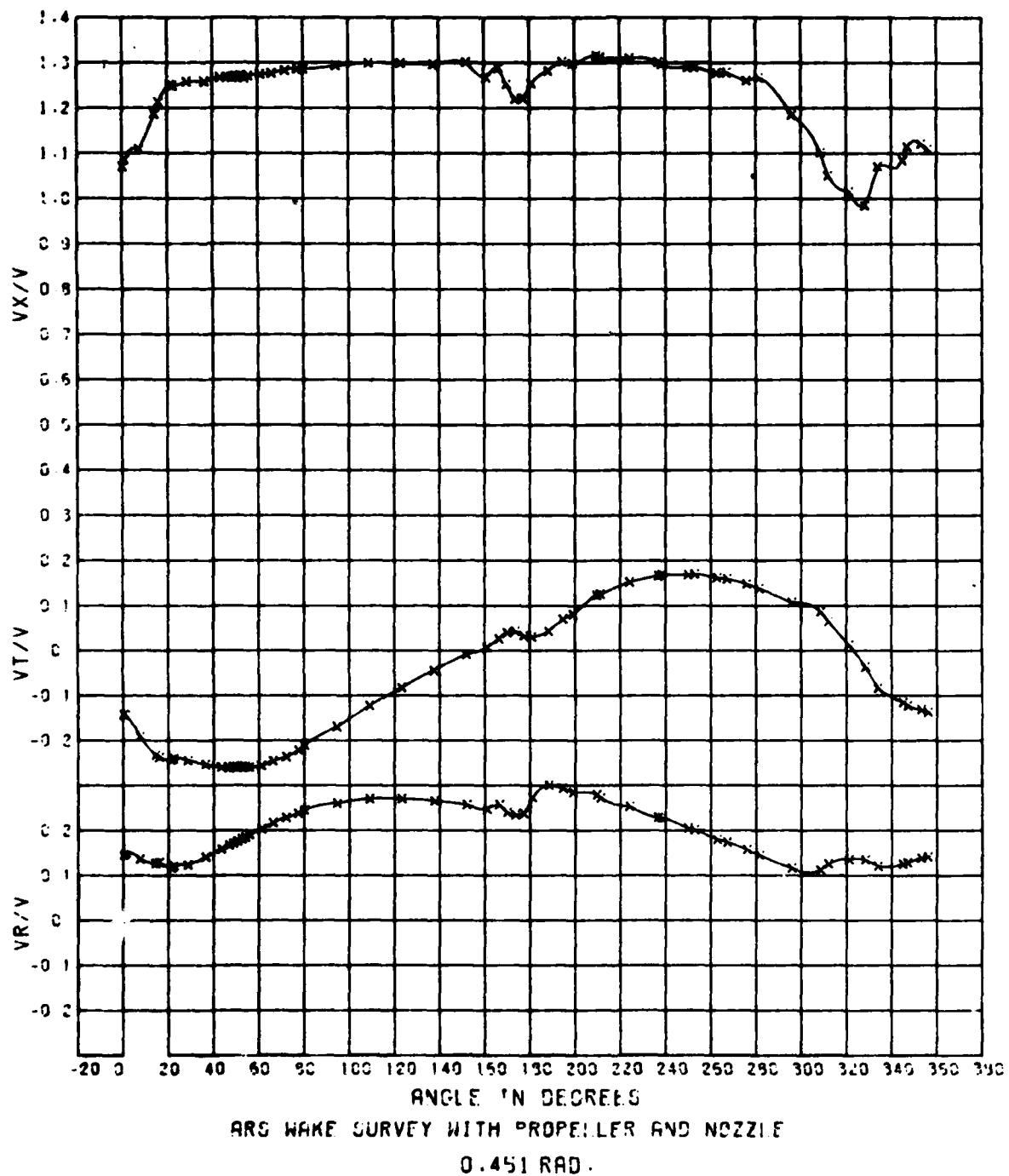
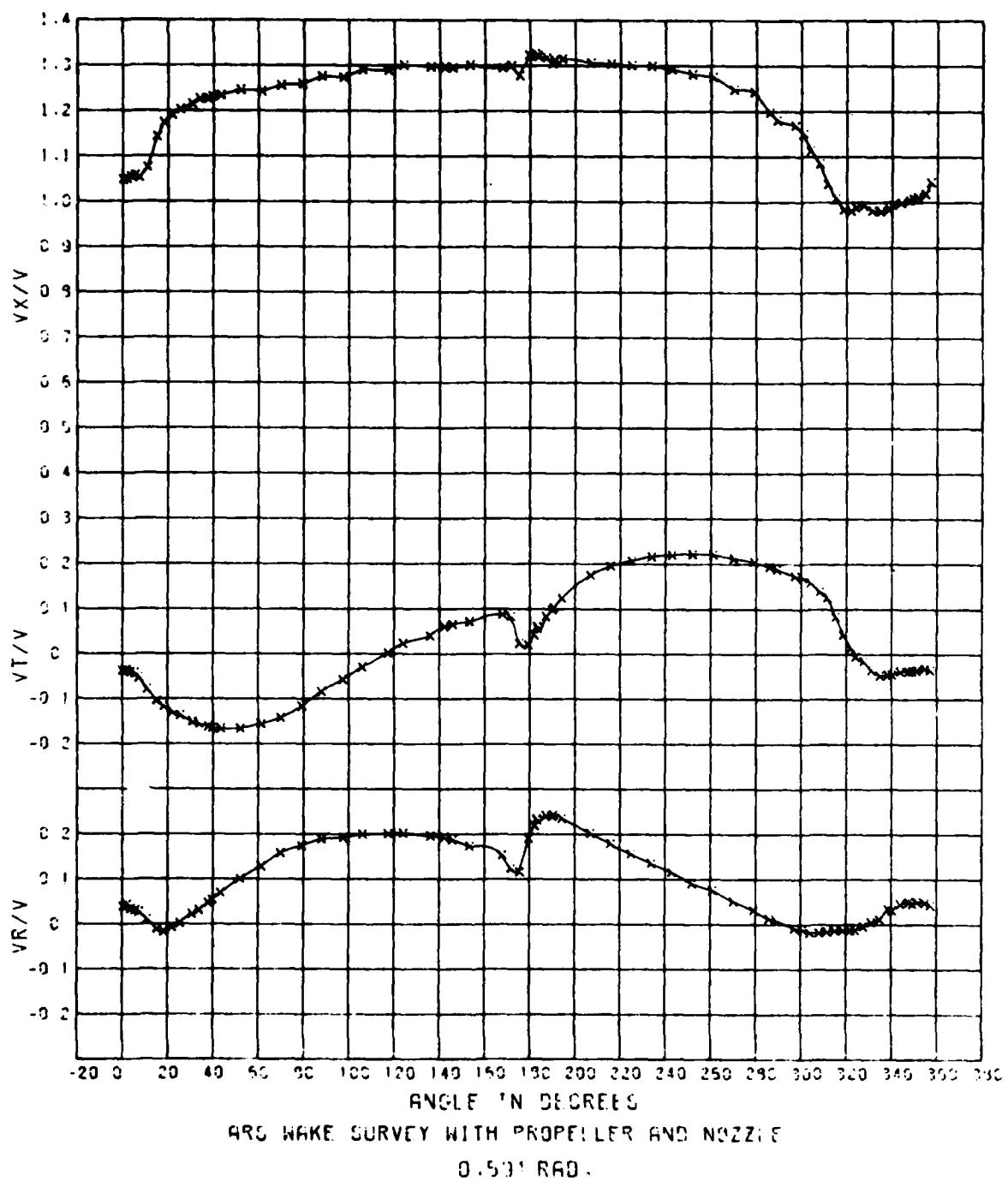


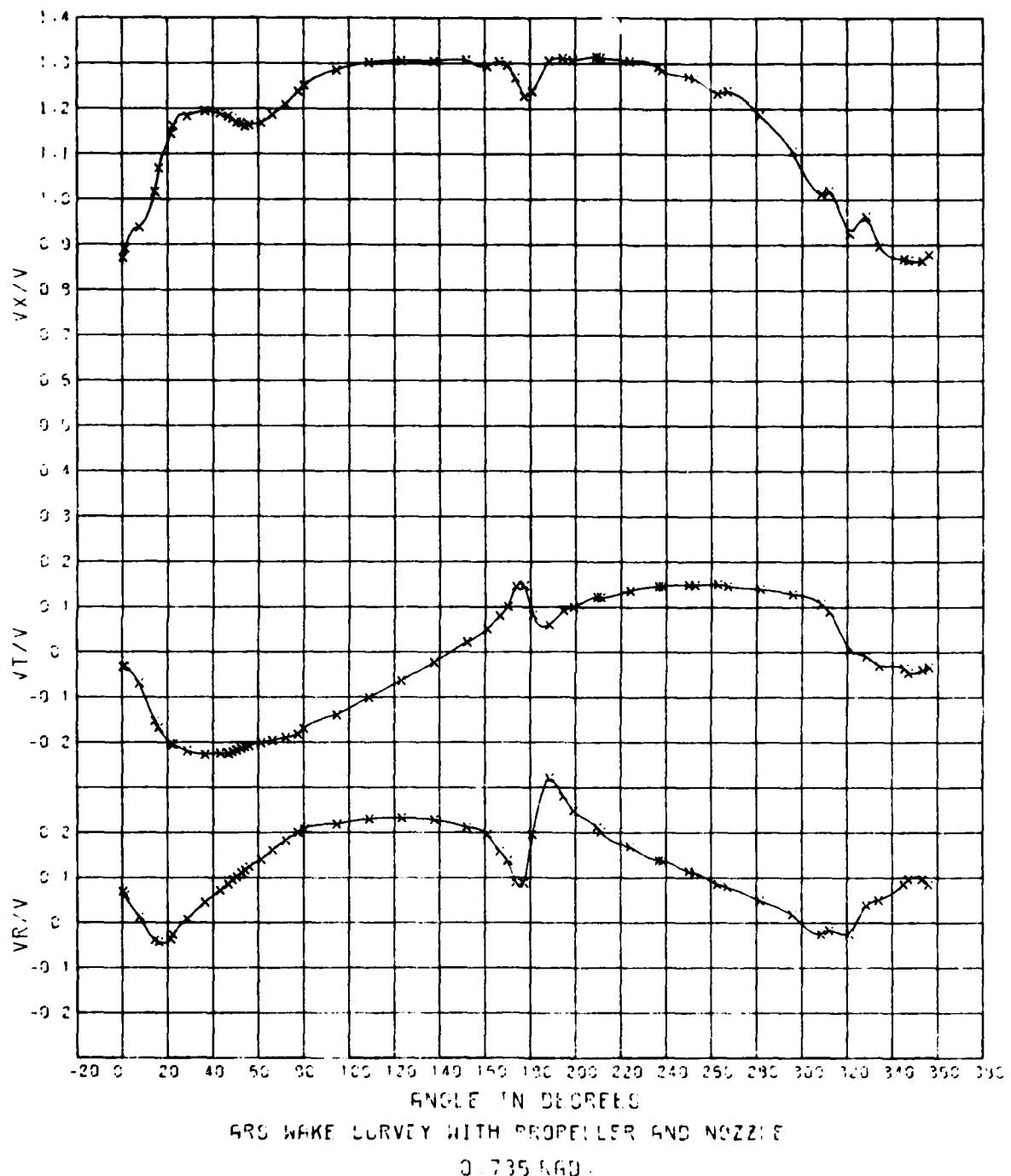
Figure 3 - Wake Survey Pitot Tube Rake Arrangement



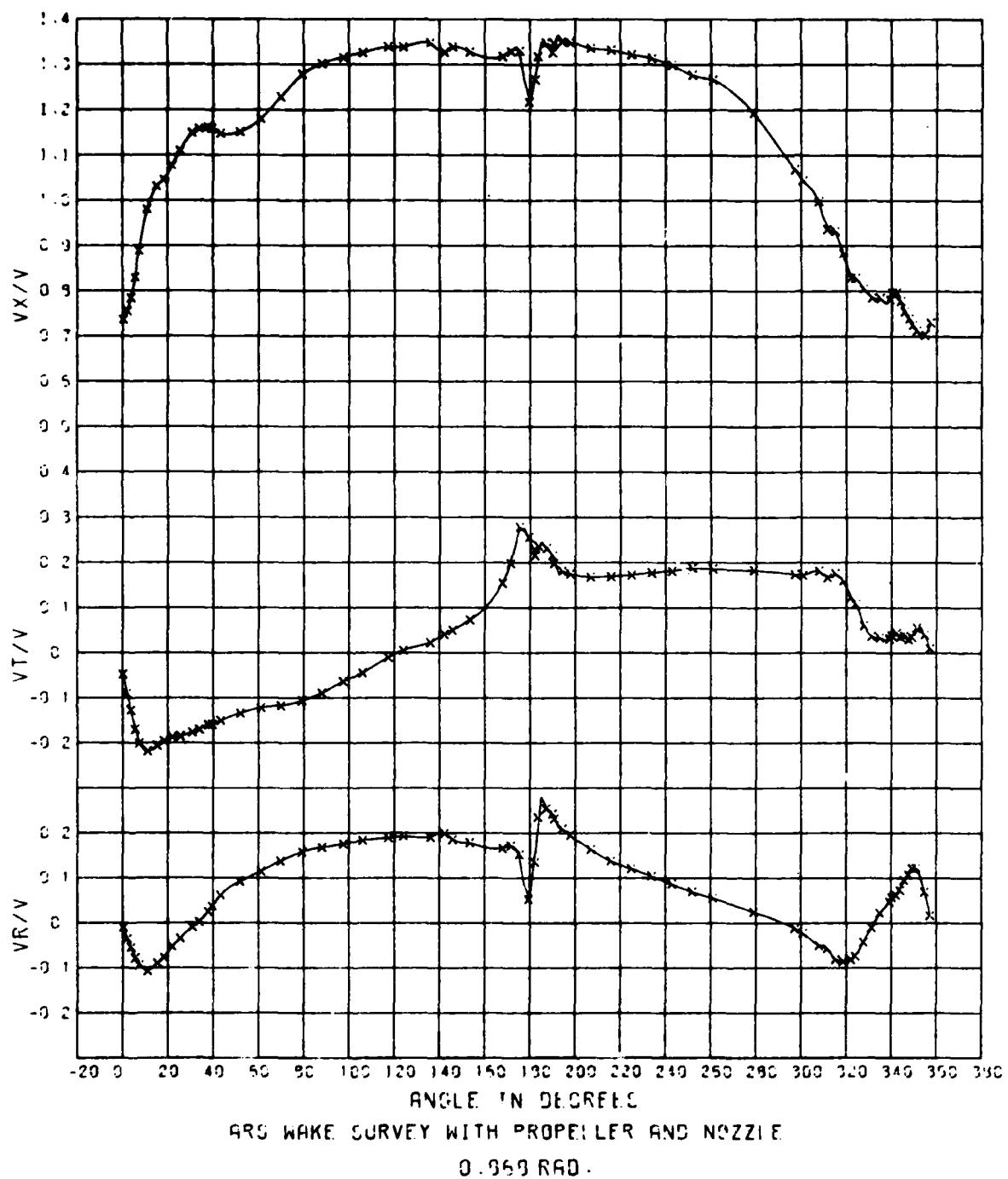
**Figure 4 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.451$  for the ARS-50 with Propeller and Nozzle**



**Figure 5 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.591$  for the ARS-50 with Propeller and Nozzle**



**Figure 6 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.735$  for the ARS-50 with Propeller and Nozzle**



**Figure 7 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.868$  for the ARS-50 with Propeller and Nozzle**

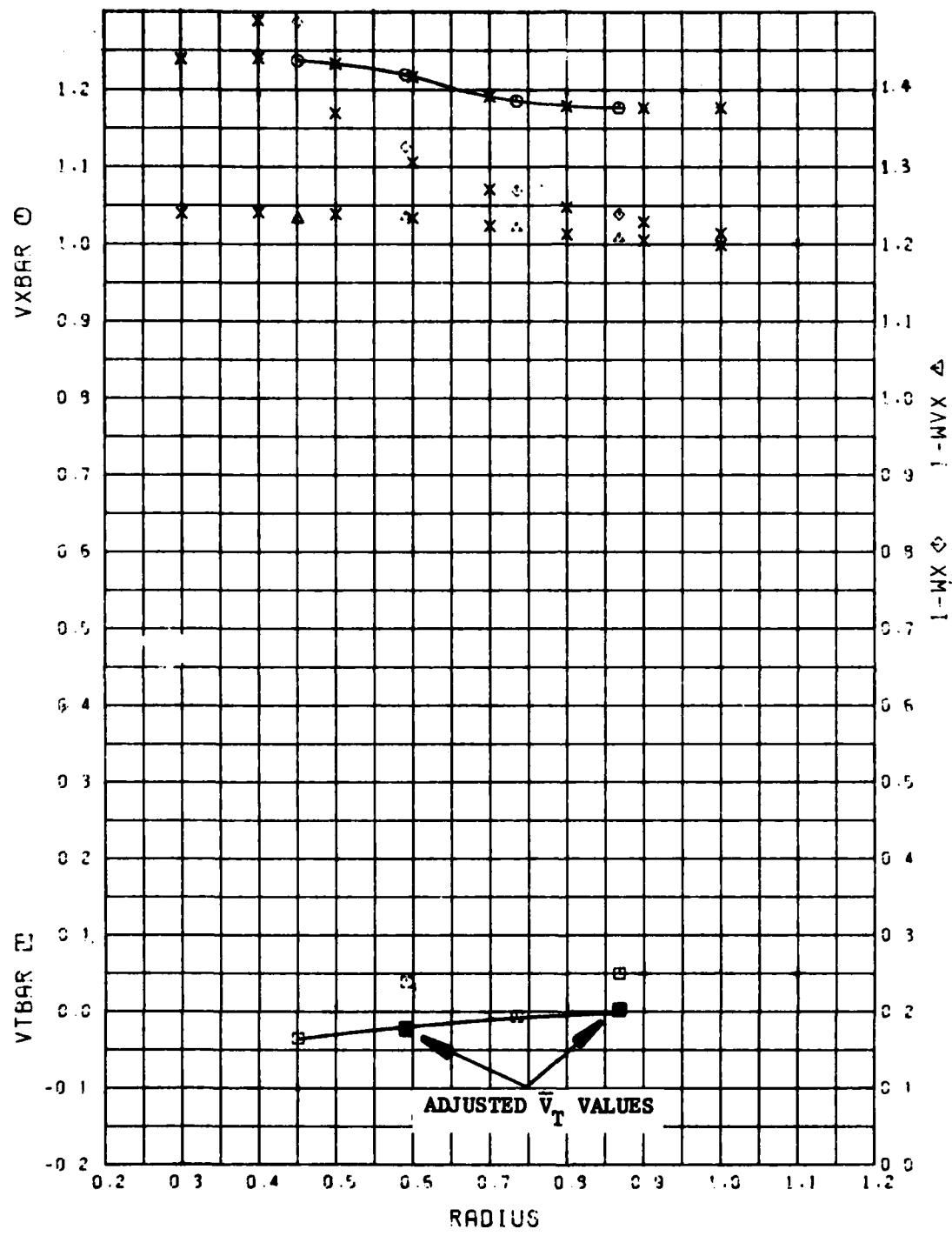


Figure 8 ~ Radial Distribution of the Mean Velocity Component Ratios for the ARS-50 with Propeller and Nozzle

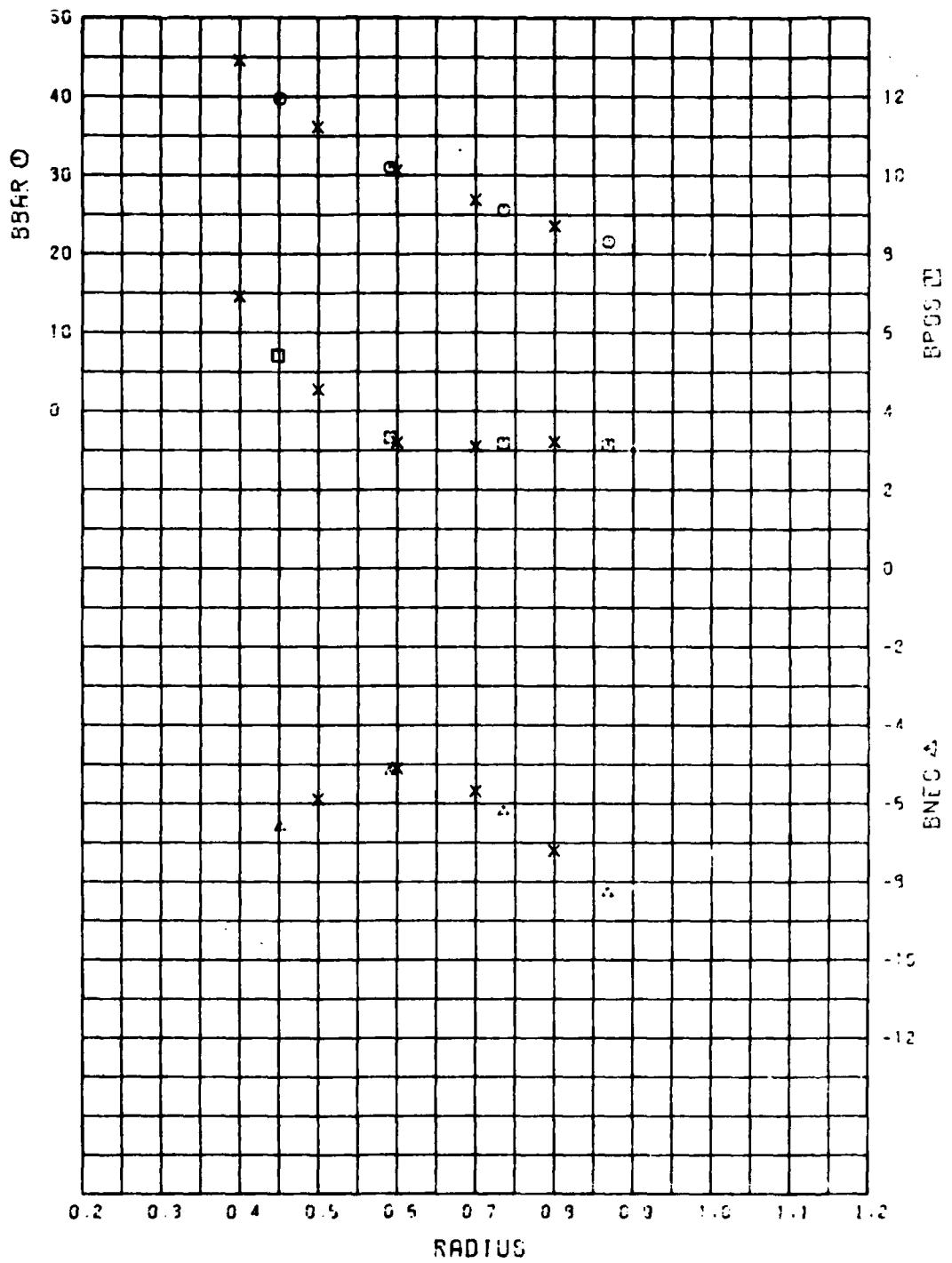
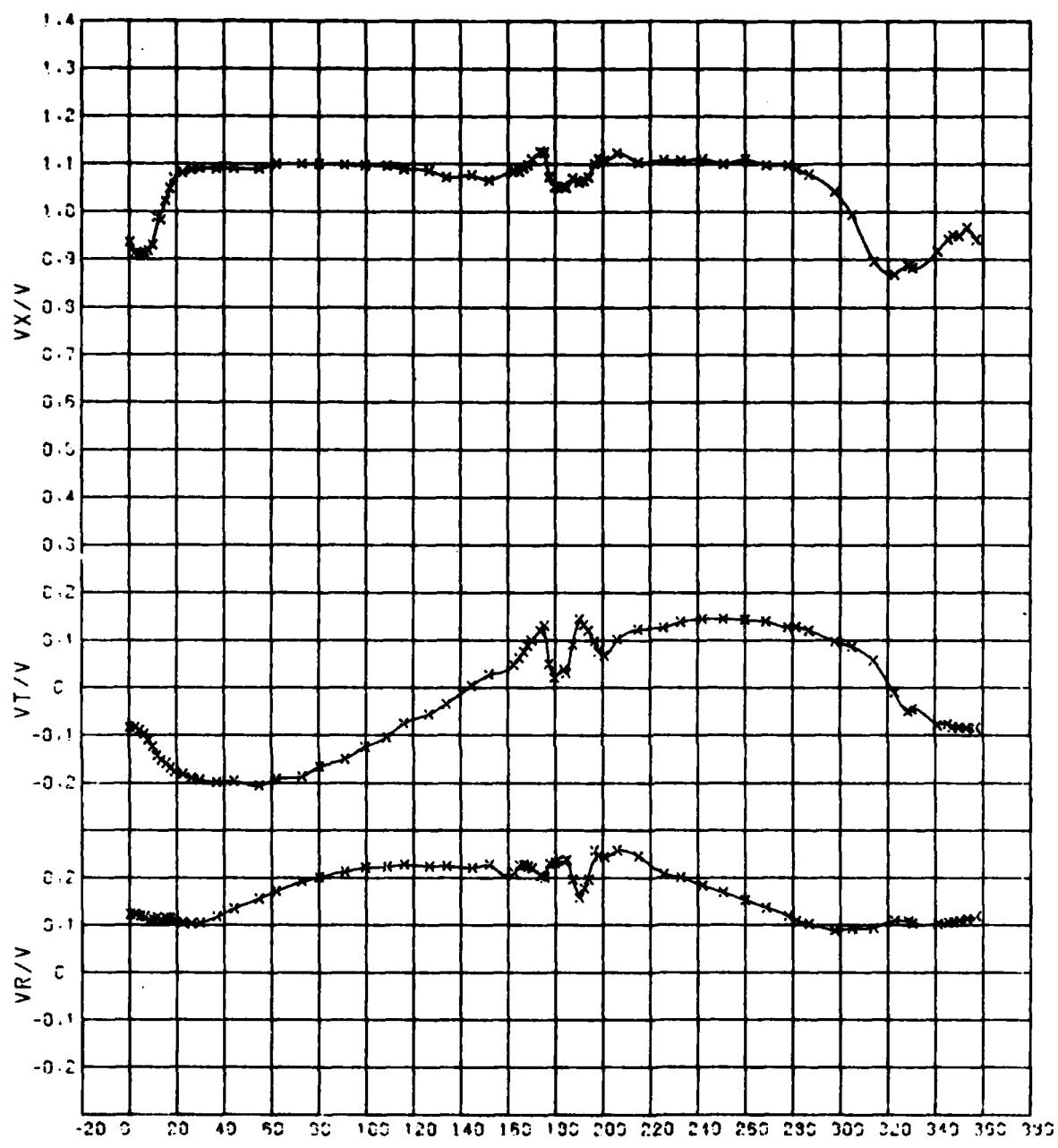


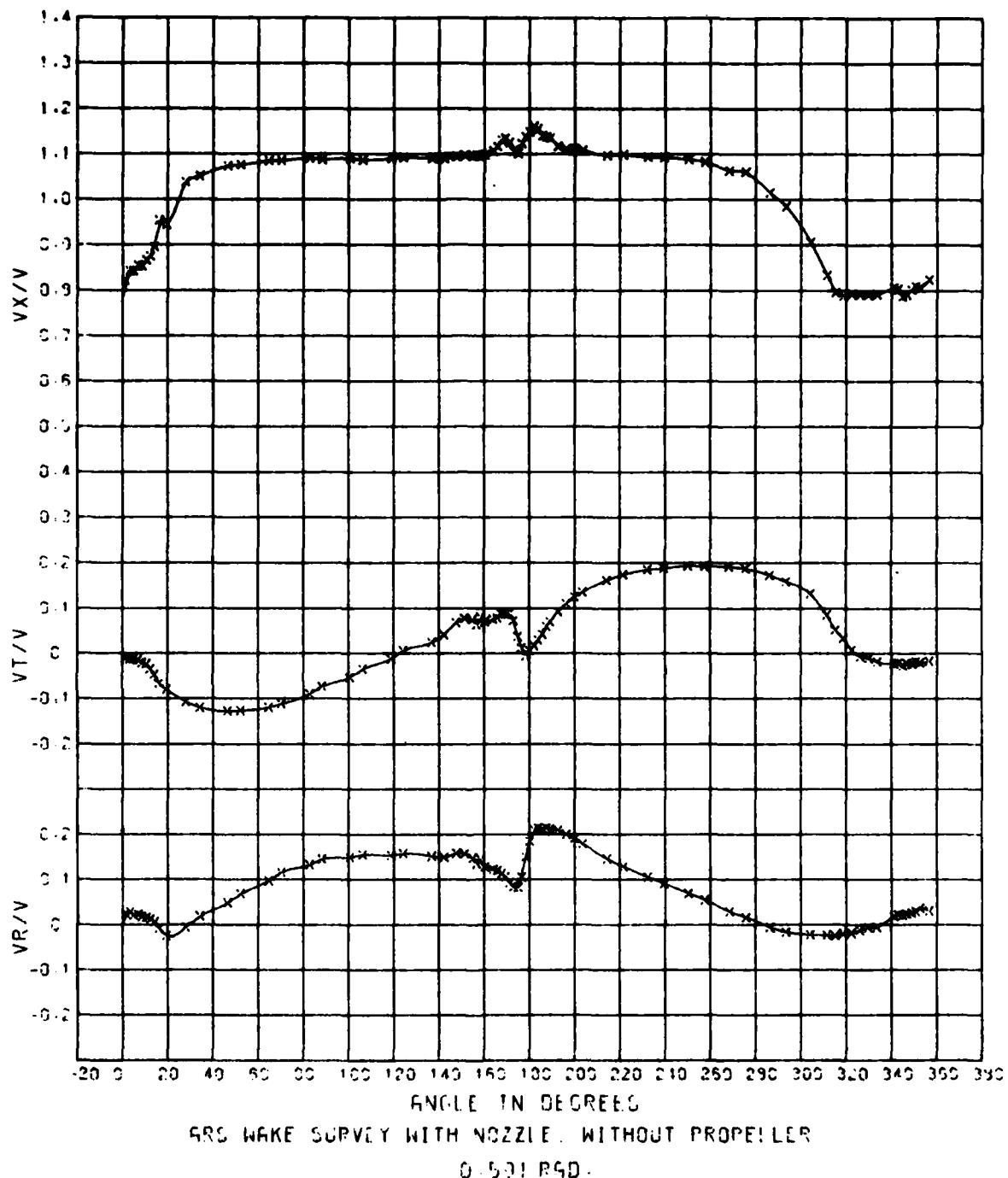
Figure 9 - Radial Distribution of the Mean Advance Angle and Advance Angle Variations for the ARS-50 with Propeller and Nozzle



ARS WAKE SURVEY WITH NOZZLE, WITHOUT PROPELLER

0.451 R/R.

Figure 10 - Circumferential Distribution of Velocity Component Ratios  
at  $r/R = 0.451$  for the ARS-50 without Propeller, with Nozzle



**Figure 11- Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.591$  for the ARS-50 without Propeller, with Nozzle**

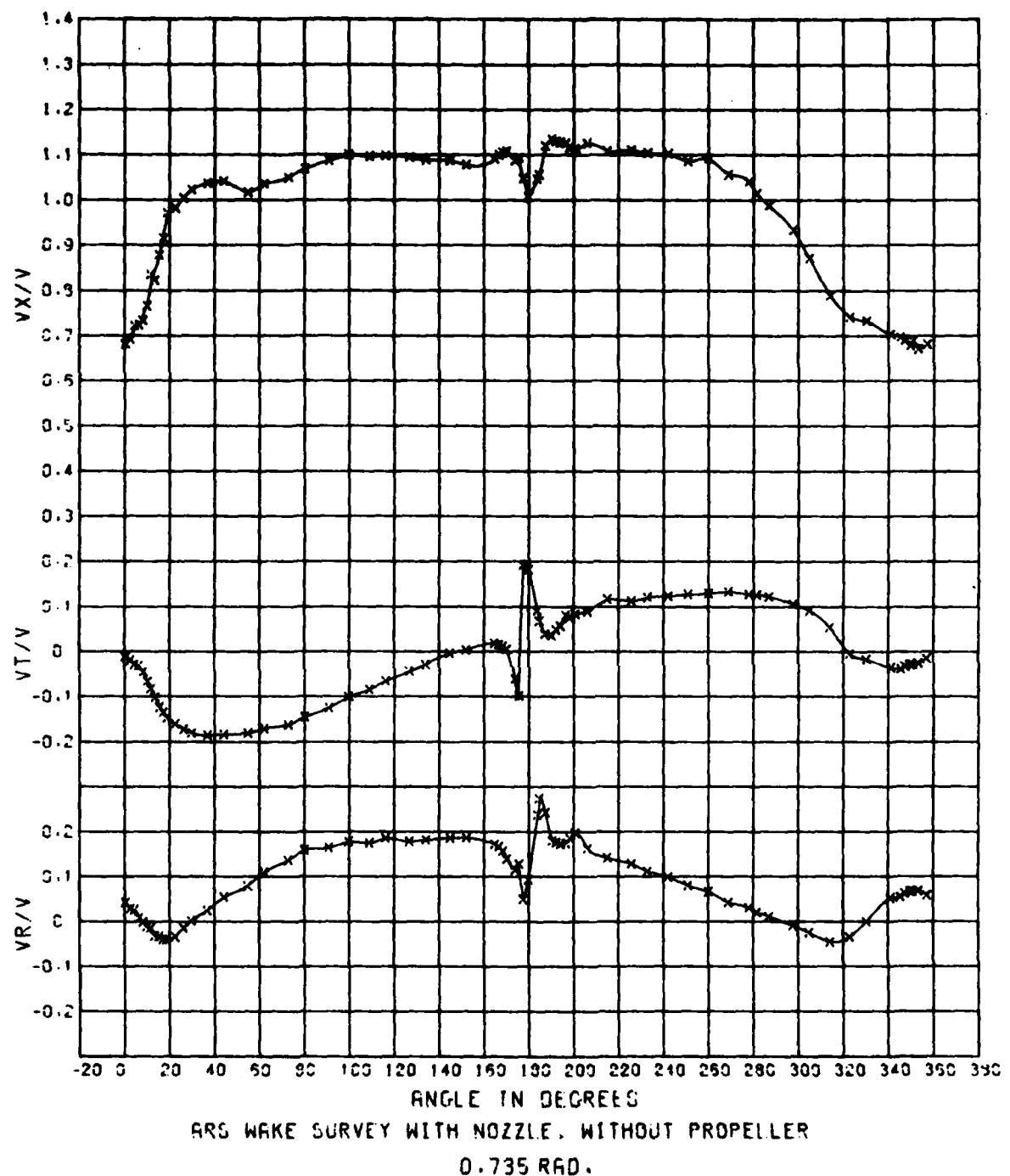
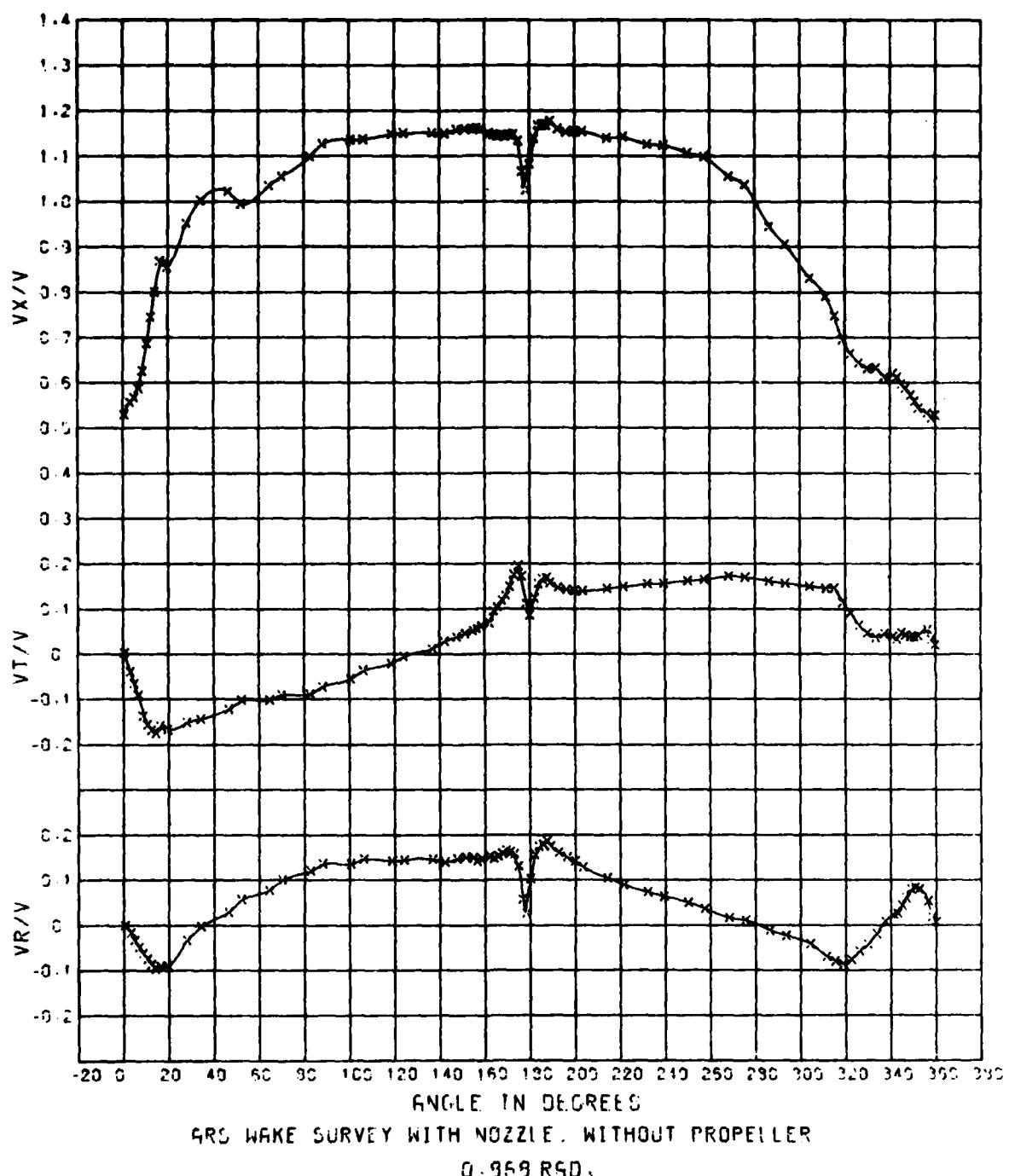


Figure 12 - Circumferential Distribution of Velocity Component Ratios  
at  $r/R = 0.735$  for the ARS-50 without Propeller, with Nozzle



**Figure 13 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.868$  for the ARS-50 without Propeller, with Nozzle**

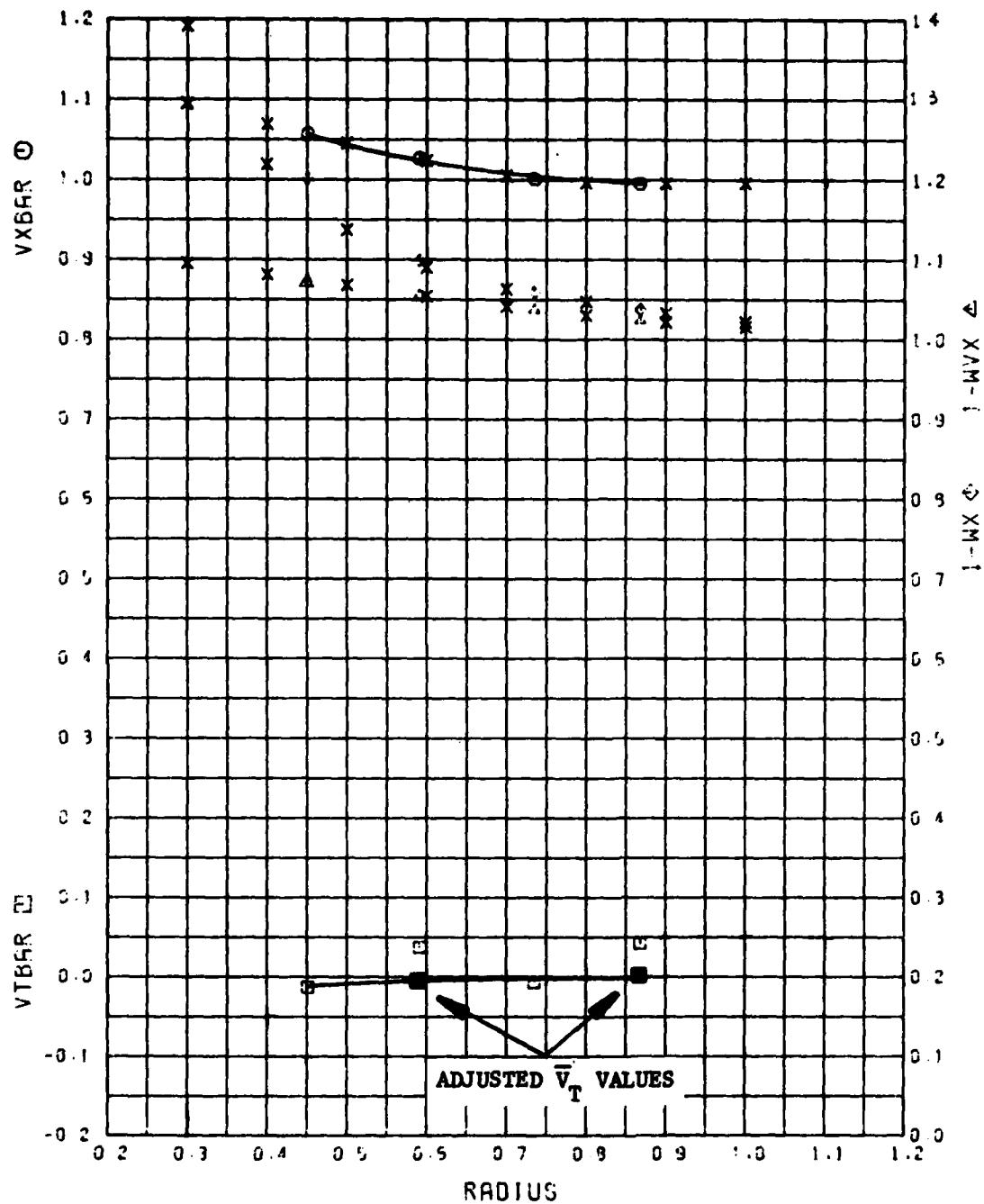


Figure 14 - Radial Distribution of the Mean Velocity Component Ratios for the ARS-50 without Propeller, with Nozzle

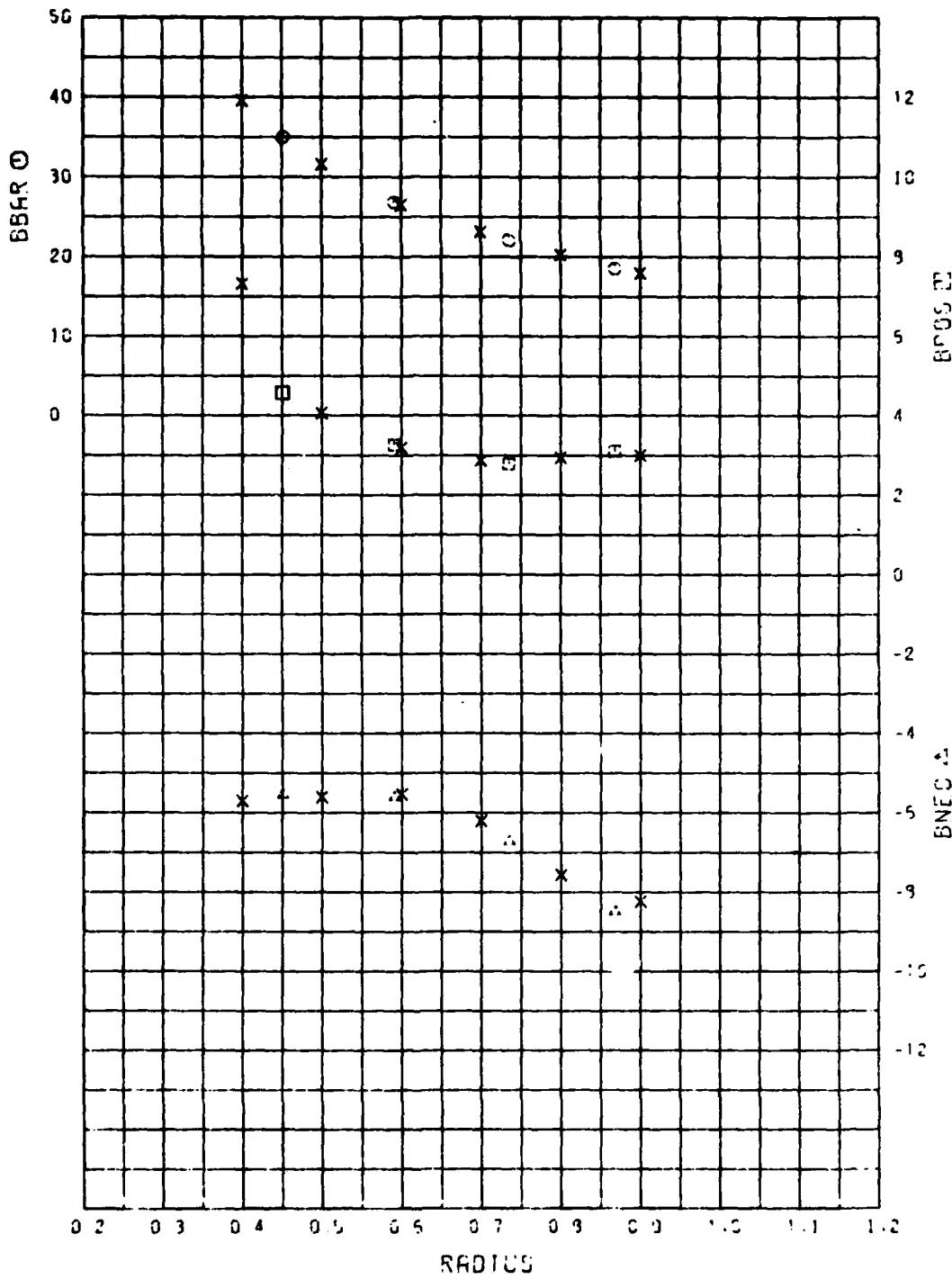


Figure 15 - Radial Distribution of the Mean Advance Angle and Advance Angle Variations for the ARS-50 without Propeller, with Nozzle

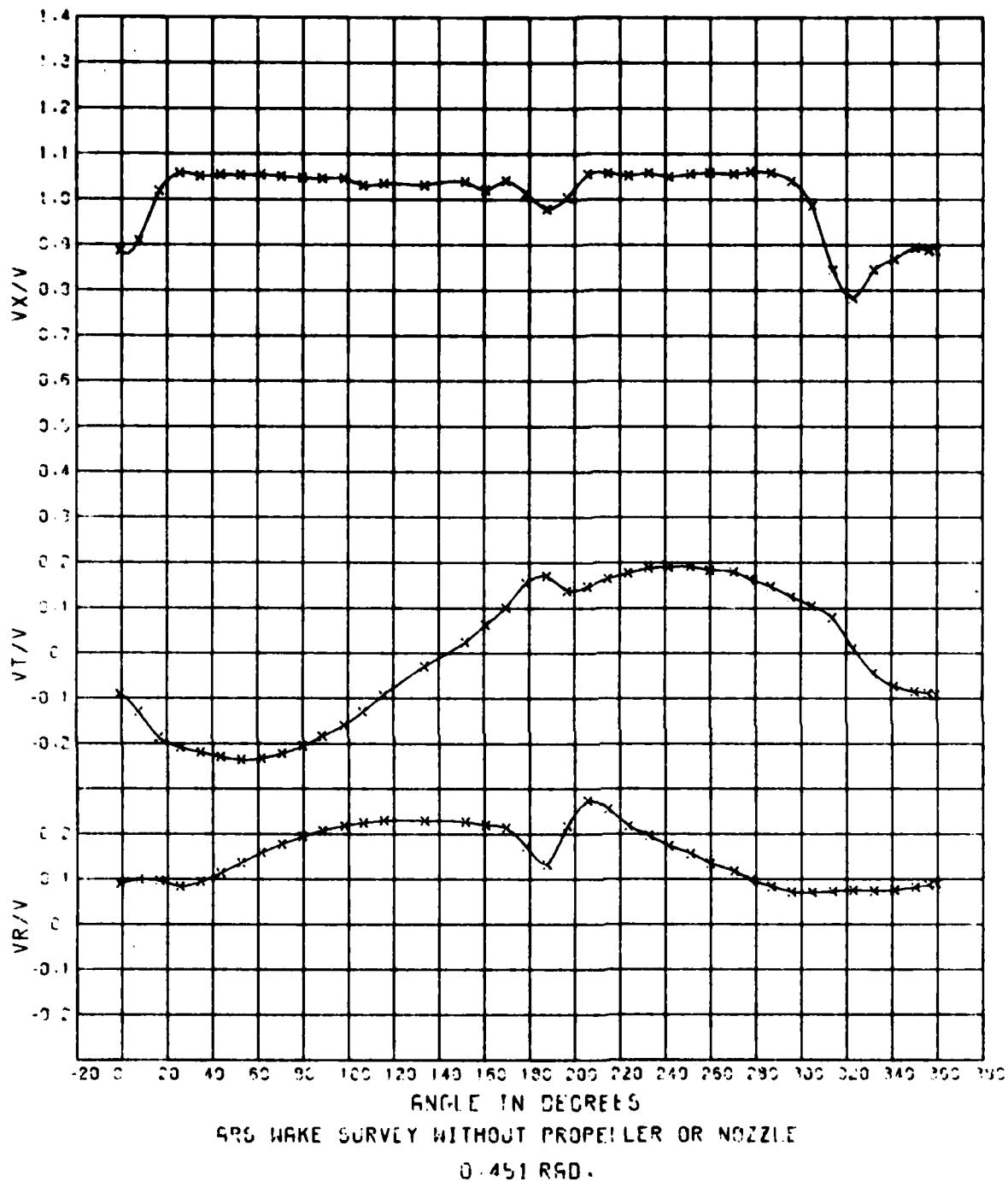
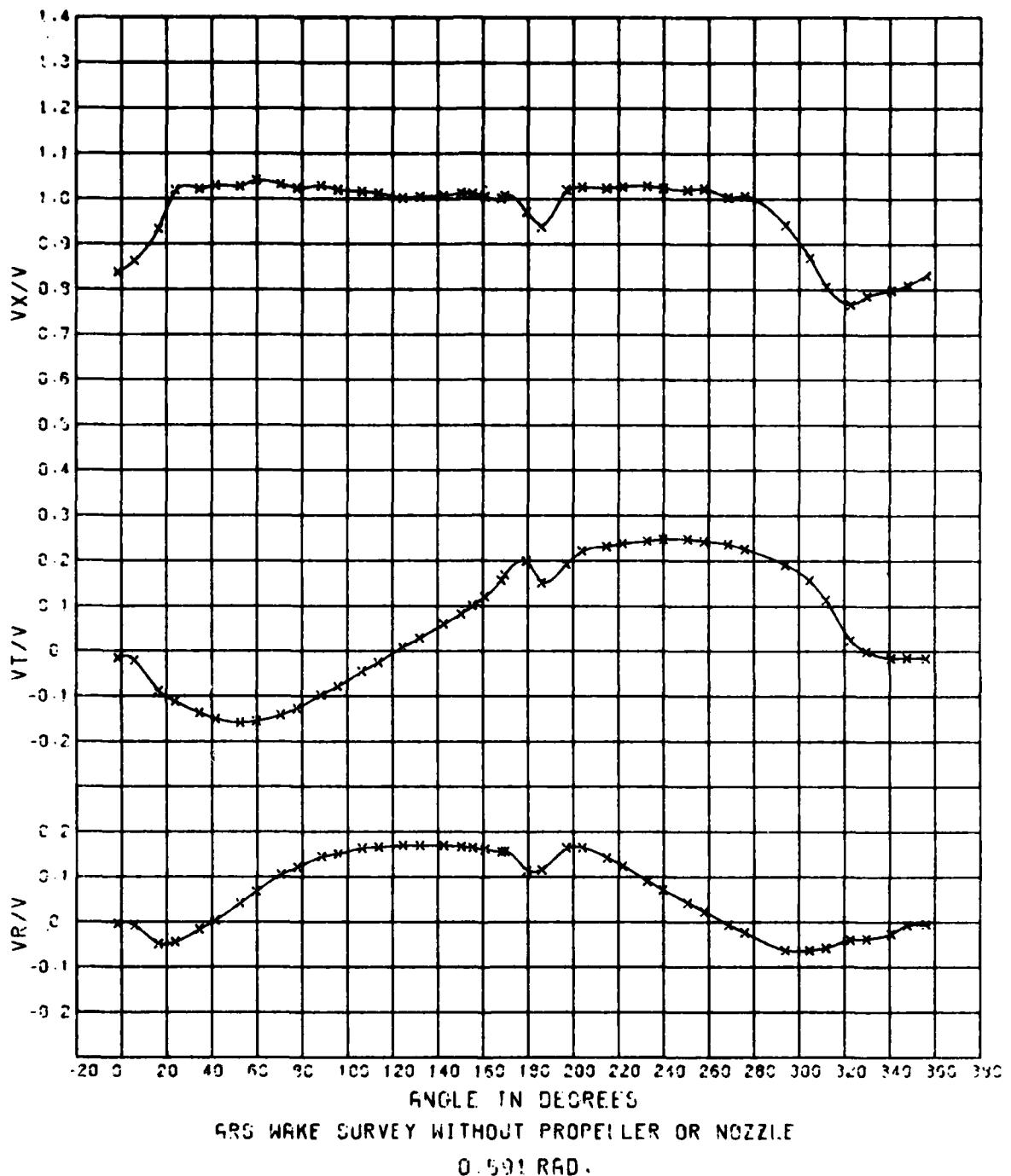
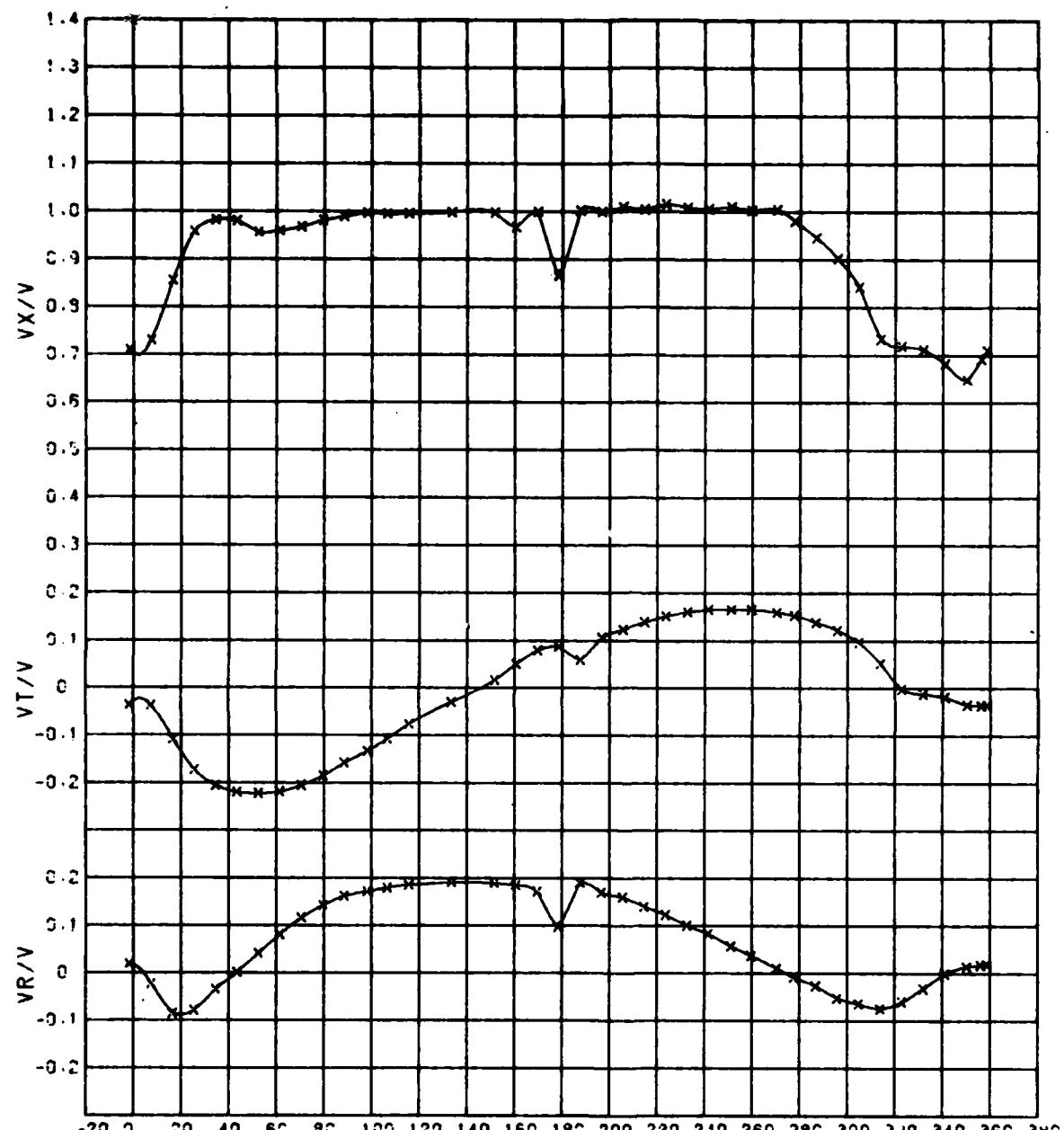


Figure 16 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.451$  for the ARS-50 without Nozzle or Propeller

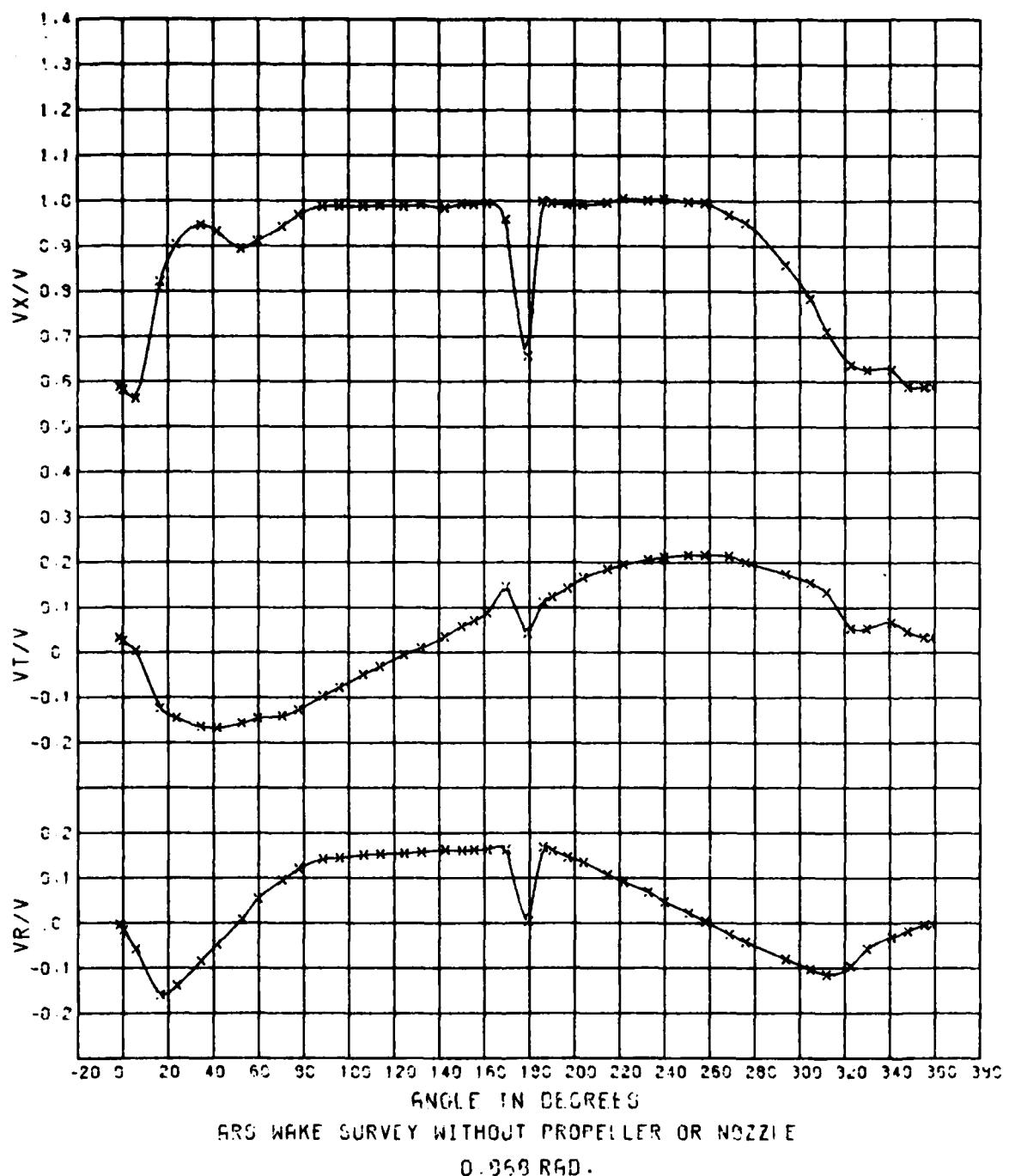


**Figure 17 - Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.591$  for the ARS-50 without Nozzle or Propeller**



ARS WAKE SURVEY WITHOUT PROPELLER OR NOZZLE  
0.735 RAD.

Figure 18- Circumferential Distribution of Velocity Component Ratios  
at  $r/R = 0.735$  for the ARS-50 without Nozzle or Propeller



**Figure 19 – Circumferential Distribution of Velocity Component Ratios at  $r/R = 0.868$  for the ARS-50 without Nozzle or Propeller**

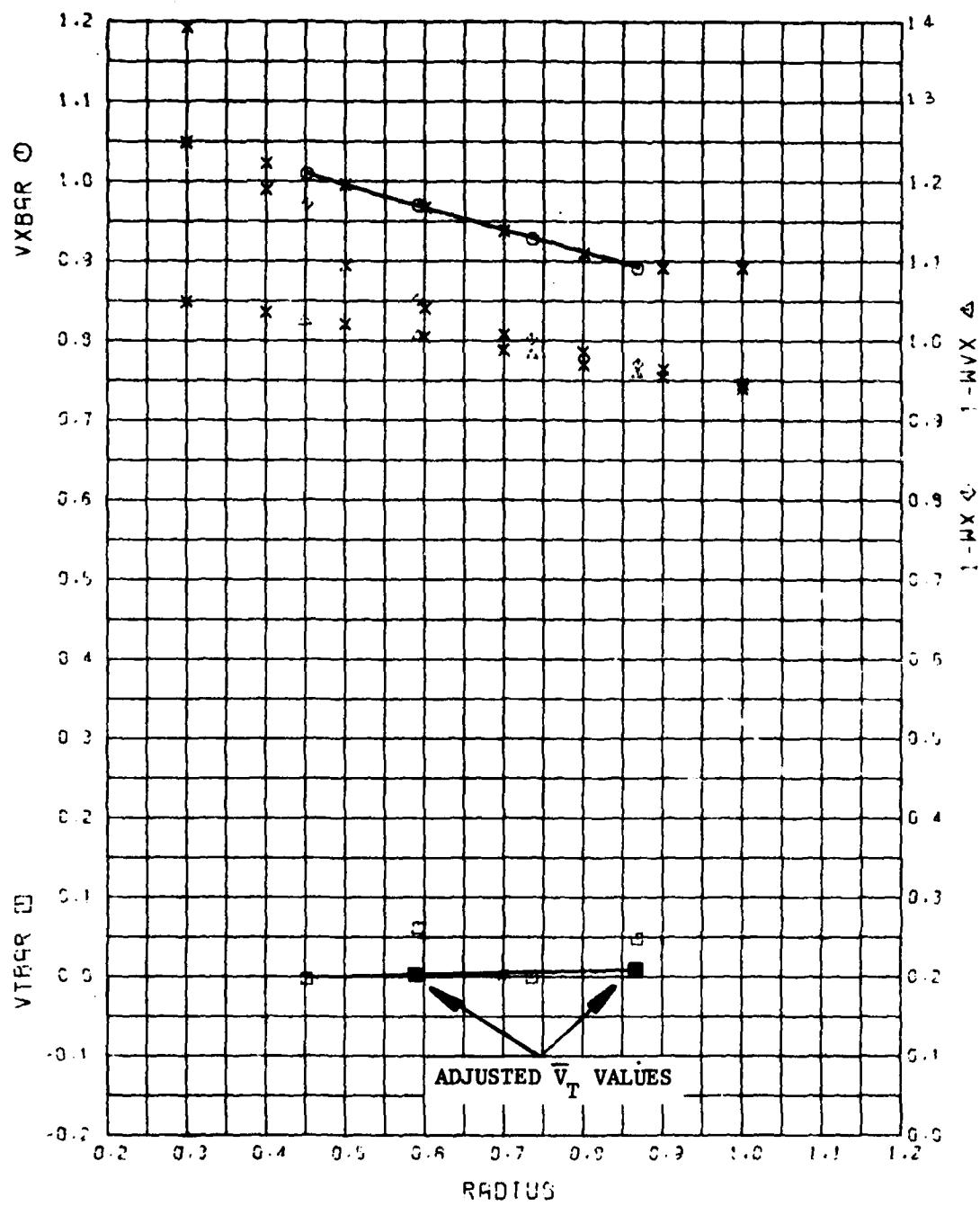


Figure 20 - Radial Distribution of the Mean Velocity Component Ratios for the ARS-50 without Nozzle or Propeller

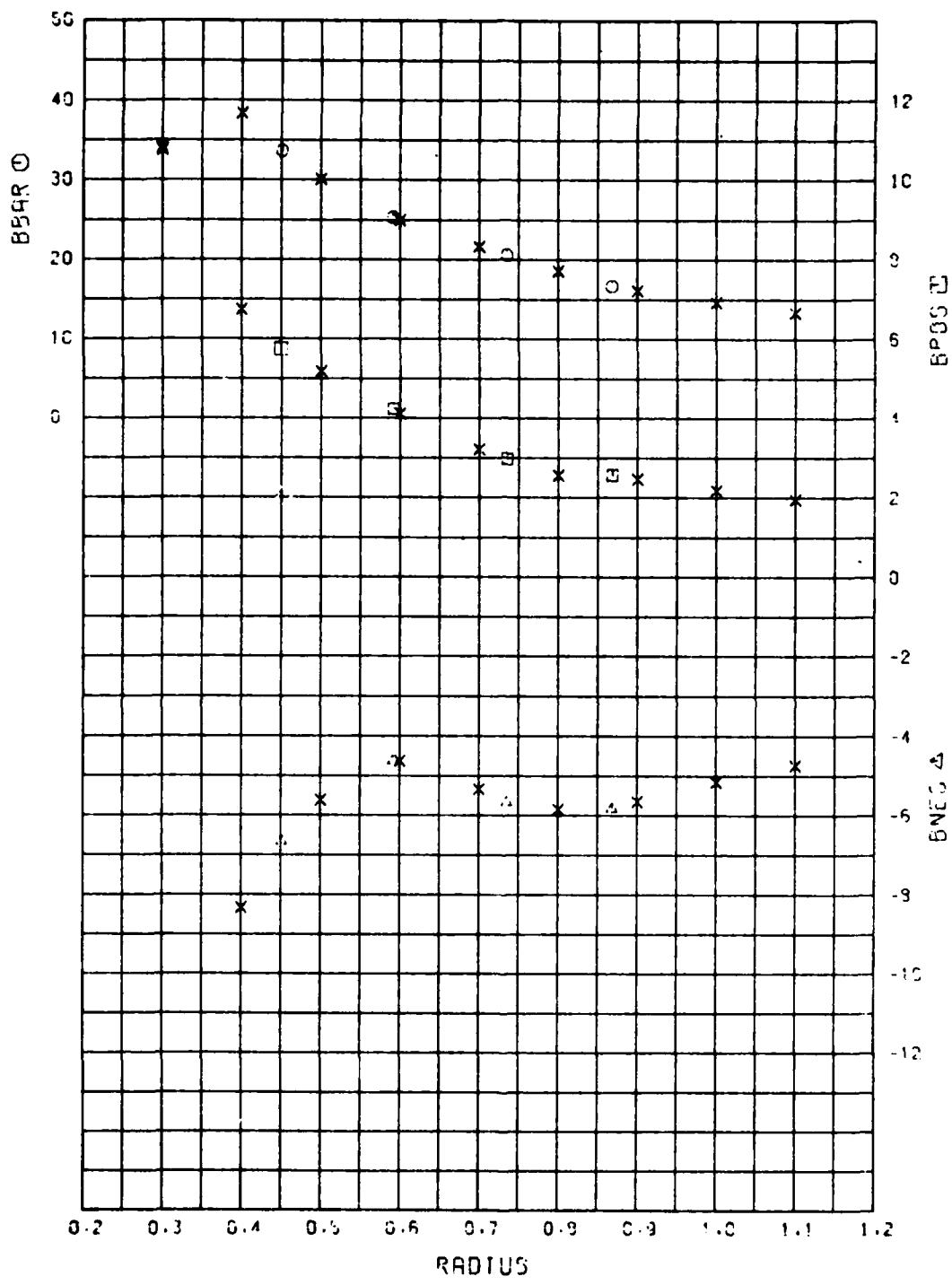


Figure 21 - Radial Distribution of the Mean Advance Angle and Advance Angle Variations for the ARS-50 without Nozzle or Propeller

ARS-50 MEAN LONGITUDINAL VELOCITY COMPONENT RATIOS

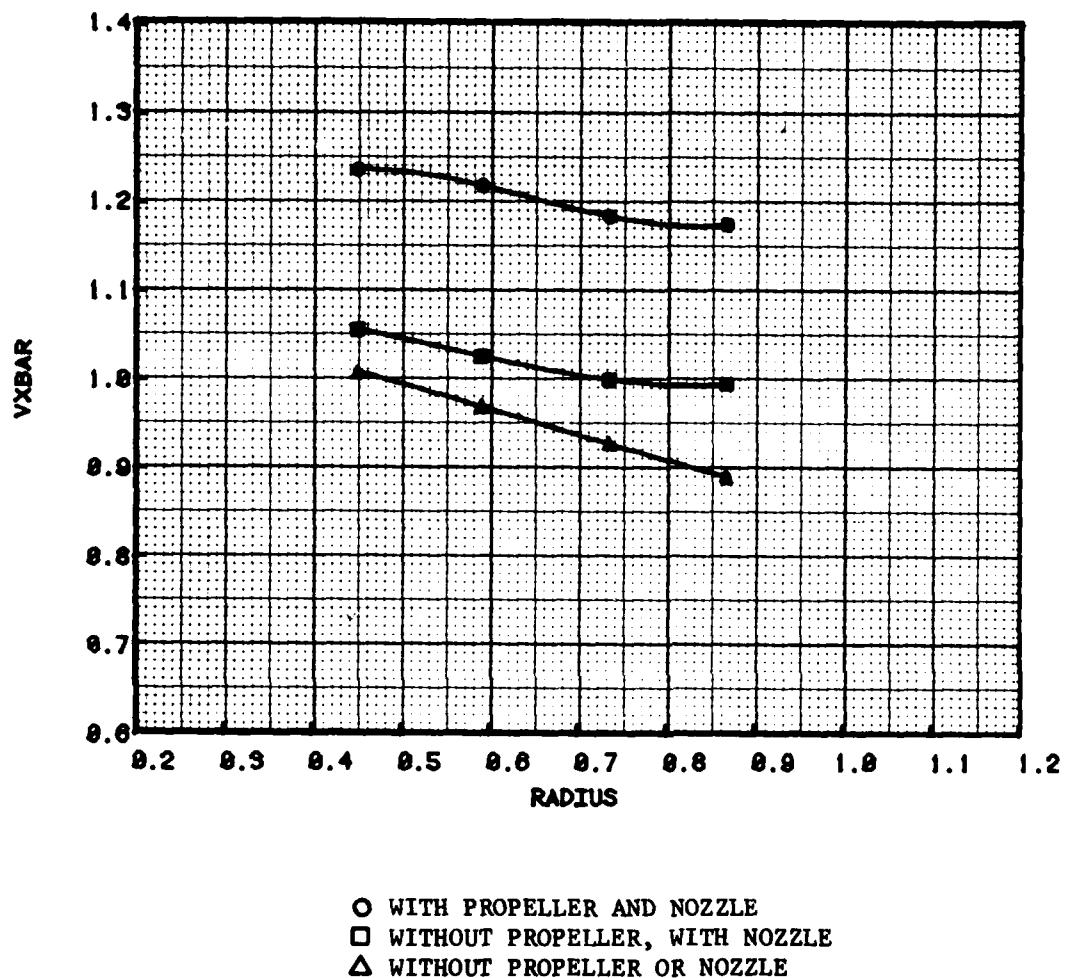


Figure 22 - Comparison Plot of the Radial Distribution of the Mean Longitudinal Velocity Component Ratio vs. Fraction of Propeller Radius for the ARS-50 in the Three Experimental Conditions

TABLE 1 - EXPERIMENTAL WAKE SURVEY DATA FOR THE ARS-50 WITH PROPELLER AND NOZZLE

ANGLE	RADIUS = .451			ANGLE	RADIUS = .451		
	VX/V	VT/V	VR/V		VX/V	VT/V	VR/V
.1	1.063	-.145	.140	312.0	1.050	.064	.126
.5	1.078	-.141	.149	321.1	1.016	.013	.136
1.1	1.086	-.144	.149	328.4	.985	-.036	.135
7.1	1.092	-.184	.133	333.9	1.071	-.084	.120
7.9	1.126	-.200	.140	345.0	1.084	-.115	.126
14.3	1.187	-.232	.127	347.0	1.115	-.122	.126
16.1	1.213	-.237	.129	352.5	1.120	-.129	.135
21.3	1.261	-.244	.120	353.6	1.123	-.134	.143
21.5	1.241	-.244	.115	356.0	1.109	-.137	.142
22.4	1.250	-.241	.121	359.8	1.037	-.141	.140
28.5	1.265	-.245	.124				
28.7	1.251	-.245	.122				
36.0	1.256	-.253	.137	ANGLE	RADIUS = .591		
36.9	1.260	-.253	.146		VX/V	VT/V	VR/V
43.4	1.268	-.260	.158	2.2	1.046	-.038	.034
46.7	1.268	-.261	.167	1.9	1.050	-.037	.043
48.6	1.268	-.260	.171	3.7	1.056	-.041	.034
50.4	1.270	-.261	.175	5.5	1.058	-.043	.031
52.3	1.270	-.259	.181	7.3	1.053	-.053	.027
54.0	1.267	-.259	.184	10.9	1.075	-.079	.009
55.8	1.271	-.260	.190	14.5	1.111	-.104	-.008
61.2	1.274	-.256	.203	15.9	1.175	-.106	-.013
65.6	1.275	-.244	.217	18.2	1.175	-.117	-.017
66.8	1.278	-.248	.217	21.8	1.191	-.129	-.007
72.1	1.283	-.237	.228	25.4	1.203	-.137	.002
77.4	1.287	-.222	.239	30.7	1.215	-.151	.023
80.1	1.286	-.211	.245	33.8	1.227	-.156	.031
94.5	1.293	-.170	.260	37.8	1.227	-.162	.047
108.8	1.299	-.123	.270	39.6	1.231	-.165	.054
123.1	1.299	-.082	.271	43.3	1.234	-.166	.069
137.5	1.296	-.044	.266	51.9	1.246	-.167	.100
151.9	1.301	-.009	.257	61.2	1.243	-.156	.129
161.0	1.267	.007	.247	69.8	1.256	-.142	.158
166.3	1.267	.023	.246	79.3	1.259	-.117	.174
166.3	1.310	.030	.267	87.9	1.275	-.084	.188
169.9	1.252	.040	.239	97.4	1.274	-.057	.192
173.6	1.219	.043	.234	106.0	1.291	-.030	.200
177.3	1.221	.033	.238	117.3	1.290	.001	.201
180.7	1.258	.036	.278	124.0	1.301	.024	.202
181.0	1.250	.026	.268	136.0	1.297	.040	.196
188.4	1.282	.043	.300	142.1	1.297	.061	.194
193.8	1.279	.060	.293	145.3	1.295	.062	.189
195.2	1.325	.080	.293	146.1	1.296	.069	.186
198.6	1.313	.089	.264	153.3	1.300	.071	.173
199.4	1.291	.073	.285	167.5	1.281	.069	.157
209.5	1.316	.123	.279	168.0	1.309	.067	.190
211.2	1.313	.126	.272	171.5	1.300	.083	.124
224.0	1.310	.153	.254	175.4	1.278	.023	.116
224.1	1.311	.151	.251	179.1	1.323	.011	.174
236.7	1.301	.166	.228	179.8	1.324	.029	.207
238.3	1.293	.168	.228	181.5	1.321	.040	.219
249.9	1.290	.168	.205	182.9	1.332	.043	.218
252.7	1.290	.170	.201	182.9	1.324	.069	.237
262.8	1.278	.162	.180	183.3	1.320	.054	.231
267.2	1.279	.159	.174	187.1	1.318	.057	.242
275.9	1.260	.148	.157	189.6	1.291	.105	.238
281.5	1.267	.138	.145	190.3	1.319	.092	.241
295.8	1.158	.102	.117	190.6	1.313	.103	.243
295.9	1.212	.112	.110	194.2	1.315	.124	.235
308.5	1.102	.087	.112	206.8	1.304	.174	.202

TABLE 1 - CONTINUED

ANGLE	RADIUS = .591	VX/V	VT/V	VR/V	ANGLE	RADIUS = .735	VX/V	VT/V	VR/V
206.8	1.310	.176	.203	.179	65.6	1.188	-.196	.160	
215.8	1.304	.195	.157	.157	66.8	1.186	-.197	.162	
224.9	1.301	.207	.135	.217	72.1	1.209	-.190	.182	
233.8	1.300	.216	.135	.136	77.4	1.239	-.182	.200	
233.8	1.299	.217	.116	.116	80.1	1.251	-.170	.204	
242.8	1.293	.220	.091	.091	94.5	1.285	-.139	.218	
251.8	1.282	.223	.076	.123.1	105.8	1.302	-.101	.230	
260.9	1.275	.221	.051	.137.5	123.1	1.307	-.064	.232	
270.1	1.248	.213	.031	.151.9	137.5	1.305	-.024	.228	
279.0	1.242	.205	.018	.161.0	151.9	1.308	.022	.212	
286.0	1.198	.194	.013	.166.3	161.0	1.293	.050	.196	
289.2	1.181	.189	.009	.166.3	166.3	1.246	.073	.171	
297.1	1.169	.174	-.009	.166.3	169.9	1.314	.087	.145	
300.7	1.151	.170	-.011	.173.6	169.9	1.297	.100	.138	
304.0	1.114	.160	-.018	.177.3	173.6	1.268	.146	.089	
308.0	1.084	.139	-.018	.180.7	181.0	1.243	.147	.087	
311.6	1.039	.126	-.016	.188.4	188.4	1.234	.094	.185	
315.1	1.009	.083	-.013	.193.8	193.8	1.306	.059	.320	
318.6	.983	.044	-.012	.195.2	198.6	1.304	.086	.278	
321.9	.983	.018	-.014	.195.2	199.4	1.312	.099	.248	
322.1	.979	.010	-.012	.209.5	209.5	1.314	.099	.249	
324.0	.989	-.006	-.013	.211.2	211.2	1.312	.122	.212	
327.6	.993	-.016	-.004	.224.0	224.1	1.301	.137	.170	
331.2	.982	-.035	.006	.224.1	236.7	1.292	.146	.138	
334.9	.980	-.047	.011	.238.3	238.3	1.286	.146	.138	
338.5	.985	-.045	.034	.249.9	249.9	1.272	.149	.114	
340.2	.994	-.045	.031	.252.7	252.7	1.268	.148	.111	
343.9	.999	-.038	.046	.262.8	262.8	1.235	.150	.085	
347.6	1.005	-.038	.049	.267.2	267.2	1.239	.147	.079	
349.2	1.008	-.037	.047	.281.5	281.5	1.186	.140	.049	
351.1	1.012	-.037	.051	.295.8	295.8	1.112	.128	.026	
354.8	1.018	-.032	.048	.295.9	295.9	1.101	.128	.011	
356.5	1.034	-.034	.043	308.5	312.0	1.012	.107	-.026	
357.9	1.054	-.036	.042	321.1	321.1	.089	-.017		
358.3	1.044	-.036	.045	328.4	.924	.005	-.026		
ANGLE	RADIUS = .735	VX/V	VT/V	VR/V	333.9	.896	-.009	.039	
.1	.874	-.033	.068	.345.0	.869	-.031	.050		
.5	.867	-.032	.070	.347.0	.866	-.036	.085		
1.1	.890	-.033	.060	.352.5	.858	-.046	.097		
7.1	.925	-.066	.021	.353.6	.871	-.035	.095		
7.9	.950	-.074	.004	.356.0	.878	-.035	.084		
14.3	1.015	-.153	-.039	.359.8	.889	-.035	.066		
16.1	1.068	-.168	-.043	308.5	321.1	.089	-.017		
21.3	1.161	-.204	-.035	328.4	.924	.005	-.026		
21.5	1.128	-.202	-.039	333.9	.896	-.031	.050		
22.4	1.162	-.205	-.027	345.0	.869	-.036	.085		
28.5	1.195	-.222	.007	347.0	.866	-.046	.097		
28.7	1.172	-.217	.008	352.5	.858	-.045	.097		
36.0	1.193	-.226	.041	353.6	.871	-.035	.095		
36.9	1.195	-.229	.049	356.0	.878	-.035	.084		
43.1	1.190	-.223	.072	359.8	.889	-.035	.066		
46.7	1.183	-.225	.085	308.5	321.1	.089	-.017		
48.6	1.179	-.222	.095	328.4	.924	.005	-.026		
50.4	1.169	-.218	.101	333.9	.896	-.031	.050		
52.3	1.169	-.214	.111	345.0	.869	-.036	.085		
54.0	1.161	-.210	.116	347.0	.866	-.128	-.055		
55.8	1.164	-.208	.124	352.5	.858	-.170	-.078		
61.2	1.168	-.201	.140	353.6	.871	-.201	-.094		
ANGLE	RADIUS = .868	VX/V	VT/V	VR/V	356.0	.878	-.219	-.108	
					359.8	.889	-.210	-.091	
					308.5	.953	-.203	-.089	
					321.1	.903	-.197	-.078	
					328.4	.976	-.187	-.053	

TABLE 1 - CONTINUED

ANGLE	RADIUS = .868	VX/V	VT/V	VR/V	ANGLE	RADIUS = .868	VX/V	VT/V	VR/V
25.4	1.110	-.186	-.035	-.010	342.1	.796	.044	.062	.062
30.7	1.149	-.177	-.010	.002	343.9	.778	.036	.073	.095
33.8	1.159	-.171	.025	.345.7	.755	.038	.107	.121	
37.8	1.162	-.160	.037	.347.6	.739	.030	.122	.122	
39.6	1.159	-.159	.062	.349.2	.725	.035	.069	.069	
43.3	1.148	-.151	.091	.351.1	.712	.056	.024	.039	
51.9	1.151	-.134	.114	.354.8	.703	.040	-.004	-.006	
61.2	1.179	-.122	.137	.356.5	.701	.024	.011	.011	
69.8	1.229	-.118	.158	.357.9	.760	-.004	-.009	-.006	
79.3	1.278	-.106	.168	.358.3	.716	-.009	.011		
87.9	1.302	-.090	.175						
97.4	1.315	-.064	.184						
106.0	1.326	-.045	.189						
117.3	1.339	-.011	.193						
124.0	1.338	.005	.190						
136.0	1.348	.023	.199						
142.1	1.327	.041	.186						
145.3	1.345	.047	.184						
146.1	1.333	.054	.184						
153.3	1.328	.073	.178						
167.5	1.308	.155	.159						
168.0	1.327	.154	.173						
171.5	1.329	.198	.172						
175.4	1.331	.278	.152						
179.1	1.227	.286	.045						
179.8	1.209	.225	.060						
181.5	1.266	.216	.124						
182.9	1.267	.214	.146						
183.4	1.318	.237	.235						
187.1	1.349	.231	.254						
189.6	1.326	.213	.234						
190.3	1.328	.218	.250						
190.6	1.348	.198	.231						
194.2	1.351	.181	.209						
197.8	1.349	.175	.195						
206.8	1.339	.167	.157						
206.8	1.334	.169	.171						
215.8	1.332	.169	.138						
224.9	1.322	.172	.121						
233.8	1.314	.177	.105						
233.8	1.314	.178	.104						
242.8	1.299	.181	.087						
251.8	1.277	.187	.069						
260.9	1.266	.186	.056						
279.0	1.194	.183	.025						
297.1	1.069	.174	-.012						
300.7	1.044	.172	-.023						
308.0	.998	.182	-.050						
311.6	.936	.167	-.057						
315.1	.932	.175	-.081						
318.6	.884	.160	-.085						
321.9	.815	.120	-.081						
322.1	.843	.126	-.082						
324.0	.828	.108	-.074						
327.6	.805	.060	-.043						
331.2	.785	.037	-.011						
334.9	.794	.035	.022						
338.5	.788	.031	.050						
339.9	.774	.032	.044						
340.2	.796	.038	.057						

TABLE 2 - LISTING OF THE MEAN VELOCITY COMPONENT RATIOS, THE MEAN ADVANCE ANGLES AND OTHER DERIVED QUANTITIES AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITH PROPELLER AND NOZZLE

	ARS WAKE SURVEY WITH PROPELLER AND NOZZLE PROPELLER DIAMETER = 10.50 FEET							JV	.932				
RADIUS	.451	.591	.735	.868	.299	.300	.400	.500	.600	.700	.800	.900	1.000
VXBAR	1.238	1.220	1.186	1.177	1.240	1.240	1.241	1.234	1.217	1.192	1.179	1.177	1.177
VTBAR	-.035	.039	-.006	.050	-.247	-.245	-.090	.005	.033	-.005	.010	.050	.050
VRBAR	-.203	.109	.126	.089	.428	.426	.264	.157	.111	.127	.114	.089	.089
1-WX	1.239	1.235	1.221	1.208	0.000	1.240	1.241	1.239	1.234	1.224	1.213	1.205	1.199
BBAR	39.80	30.99	25.63	21.58	58.44	58.27	41.60	36.13	30.63	26.85	23.53	20.89	18.98
BPOS	5.47	3.32	3.17	3.14	14.18	14.10	6.92	4.55	3.20	3.09	3.21	3.04	2.77
THETA	57.50	52.50	97.50	107.50	20.00	20.00	20.00	52.50	52.50	95.00	100.00	110.00	110.00
BNEG	-6.61	-5.19	-6.21	-8.29	-19.99	-19.79	-8.53	-5.89	-5.11	-5.69	-7.21	-8.05	-7.37
THETA	=325.00	317.50	0.00	352.50	177.50	325.00	315.00	317.50	342.50	352.50	352.50	352.50	352.50

VXBAR IS CIRCUMFERENTIAL MEAN LONGITUDINAL VELOCITY.  
 VTBAR IS CIRCUMFERENTIAL MEAN TANGENTIAL VELOCITY.  
 VRBAR IS CIRCUMFERENTIAL MEAN RADIAL VELOCITY.  
 1-WX IS VOLUMETRIC MEAN WAKE VELOCITY WITHOUT TANGENTIAL CORRECTION.  
 BBAR IS VOLUMETRIC MEAN WAKE VELOCITY WITH TANGENTIAL CORRECTION.  
 1-WX IS MEAN ANGLE OF ADVANCE.  
 BBAR IS MEAN ANGLE OF ADVANCE.  
 BPOS IS VARIATION BETWEEN THE MAXIMUM AND MEAN ADVANCE ANGLES (DELTA BETA PLUS).  
 BNEG IS VARIATION BETWEEN THE MINIMUM AND MEAN ADVANCE ANGLES (DELTA BETA MINUS).  
 ZNC IS ANGLE IN DEGREES AT WHICH CORRESPONDING BPOS OR BNEG OCCURS.  
 THETA

TABLE 3 - HARMONIC ANALYSIS OF THE LONGITUDINAL VELOCITY COMPONENT RATIOS AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITH PROPELLER AND NOZZLE

ARS WAKE SURVEY WITH PROPELLER AND NOZZLE PROPELLER DIAMETER = 10.50 FEET									JV	.932	
HARMONIC	=	1	2	3	4	5	6	7	8		
RADIUS = .451											
AMPLITUDE =	.0913	.0680	.0318	.0188	.0142	.0099	.0119	.0122			
PHASE ANGLE =	293.6	320.3	10.2	5.3	107.8	215.4	196.4	250.5			
RADIUS = .591											
AMPLITUDE =	.1271	.0678	.0347	.0183	.0008	.0023	.0078	.0052			
PHASE ANGLE =	287.4	319.9	346.6	3.7	37.1	190.6	212.9	237.6			
RADIUS = .735											
AMPLITUDE =	.1737	.0837	.0345	.0311	.0150	.0232	.0099	.0079			
PHASE ANGLE =	285.6	307.5	349.1	331.5	311.3	271.2	249.6	260.7			
RADIUS = .868											
AMPLITUDE =	.2356	.1134	.0456	.0387	.0182	.0222	.0112	.0112			
PHASE ANGLE =	285.7	304.1	337.6	340.4	328.2	300.1	265.2	261.6			
RADIUS = .299											
AMPLITUDE =	.0667	.0856	.0454	.0328	.0301	.0459	.0201	.0312			
PHASE ANGLE =	310.3	307.8	55.3	334.0	99.9	247.0	200.3	260.4			
RADIUS = .300											
AMPLITUDE =	.0668	.0854	.0452	.0326	.0300	.0455	.0200	.0310			
PHASE ANGLE =	310.1	307.9	55.1	334.2	99.9	246.9	200.2	260.4			
RADIUS = .400											
AMPLITUDE =	.0811	.0716	.0330	.0212	.0194	.0181	.0143	.0172			
PHASE ANGLE =	297.8	317.1	25.7	355.3	105.4	232.7	196.5	254.9			
RADIUS = .500											
AMPLITUDE =	.1027	.0664	.0324	.0173	.0043	.0058	.0100	.0087			
PHASE ANGLE =	290.7	321.8	358.5	10.4	109.3	188.1	198.7	245.1			
RADIUS = .600											
AMPLITUDE =	.1294	.0682	.0344	.0188	.0015	.0036	.0078	.0053			
PHASE ANGLE =	287.2	318.9	347.3	358.9	331.8	228.5	216.2	240.2			
RADIUS = .700											
AMPLITUDE =	.1604	.0781	.0335	.0281	.0125	.0203	.0093	.0071			
PHASE ANGLE =	285.8	309.6	350.3	333.2	309.3	267.1	243.5	258.1			
RADIUS = .800											
AMPLITUDE =	.2017	.0966	.0384	.0355	.0177	.0247	.0108	.0094			
PHASE ANGLE =	285.5	305.1	344.3	333.4	317.4	281.0	258.3	262.5			
RADIUS = .900											
AMPLITUDE =	.2356	.1134	.0456	.0387	.0182	.0222	.0112	.0112			
PHASE ANGLE =	285.7	304.1	337.6	340.4	328.2	300.1	265.2	261.6			
RADIUS = 1.000											
AMPLITUDE =	.2356	.1134	.0456	.0387	.0182	.0222	.0112	.0112			
PHASE ANGLE =	285.7	304.1	337.6	340.4	328.2	300.1	265.2	261.6			

TABLE 4 - HARMONIC ANALYSIS OF THE TANGENTIAL VELOCITY COMPONENT RATIOS AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITH PROPELLER AND NOZZLE

ARS WAKE SURVEY WITH PROPELLER AND NOZZLE PROPELLER DIAMETER = 10.50 FEET									JV = .932
HARMONIC ANALYSES OF TANGENTIAL VELOCITY COMPONENT RATIOS (VT/V)									
HARMONIC	1	2	3	4	5	6	7	8	
RADIUS = .451									
AMPLITUDE =	.2058	.0366	.0038	.0056	.0069	.0028	.0061	.0063	
PHASE ANGLE =	212.4	225.3	91.2	294.8	25.1	110.8	81.8	136.0	
RADIUS = .591									
AMPLITUDE =	.1756	.0369	.0201	.0124	.0204	.0036	.0140	.0047	
PHASE ANGLE =	213.6	238.0	63.8	351.4	64.6	83.7	94.8	189.5	
RADIUS = .735									
AMPLITUDE =	.1781	.0319	.0011	.0136	.0132	.0155	.0088	.0091	
PHASE ANGLE =	210.8	180.5	119.9	101.4	55.7	107.8	69.3	131.5	
RADIUS = .868									
AMPLITUDE =	.1825	.0423	.0358	.0144	.0155	.0204	.0076	.0183	
PHASE ANGLE =	216.1	181.3	236.3	146.5	230.3	118.3	178.0	131.8	
RADIUS = .299									
AMPLITUDE =	.2754	.0561	.0548	.0359	.0314	.0157	.0201	.0247	
PHASE ANGLE =	208.9	160.1	236.9	173.1	269.2	127.5	299.9	103.8	
RADIUS = .300									
AMPLITUDE =	.2748	.0558	.0543	.0356	.0310	.0156	.0199	.0245	
PHASE ANGLE =	208.9	160.5	236.9	173.2	269.3	127.5	300.0	103.8	
RADIUS = .400									
AMPLITUDE =	.2248	.0360	.0118	.0080	.0094	.0055	.0031	.0105	
PHASE ANGLE =	211.4	205.5	228.9	205.3	298.2	123.3	358.0	117.3	
RADIUS = .500									
AMPLITUDE =	.1916	.0384	.0133	.0100	.0133	.0018	.0103	.0046	
PHASE ANGLE =	213.2	235.9	67.5	328.5	55.3	83.3	93.0	165.2	
RADIUS = .600									
AMPLITUDE =	.1757	.0319	.0194	.0112	.0207	.0045	.0136	.0046	
PHASE ANGLE =	213.2	234.3	63.7	358.7	63.6	89.0	91.8	183.6	
RADIUS = .700									
AMPLITUDE =	.1773	.0294	.0072	.0116	.0172	.0132	.0105	.0072	
PHASE ANGLE =	210.7	189.4	66.8	87.6	56.7	105.2	70.1	136.1	
RADIUS = .800									
AMPLITUDE =	.1798	.0372	.0151	.0152	.0019	.0186	.0047	.0133	
PHASE ANGLE =	212.5	175.5	234.7	120.9	61.5	112.6	94.4	129.8	
RADIUS = .900									
AMPLITUDE =	.1825	.0423	.0358	.0144	.0155	.0204	.0076	.0183	
PHASE ANGLE =	216.1	181.3	236.3	146.5	230.3	118.3	178.0	131.8	
RADIUS = 1.000									
AMPLITUDE =	.1825	.0423	.0358	.0144	.0155	.0204	.0076	.0183	
PHASE ANGLE =	216.1	181.3	236.3	146.5	230.3	118.3	178.0	131.8	

TABLE 5 - EXPERIMENTAL WAKE SURVEY DATA FOR THE ARS-50 WITHOUT PROPELLER,  
WITH NOZZLE

ANGLE	RADIUS = .451			ANGLE	RADIUS = .451		
	VX/V	VT/V	VR/V		VX/V	VT/V	VR/V
.3	.923	-.084	.122	277.9	1.098	.128	.119
.3	.948	-.084	.123	281.4	1.090	.129	.109
2.6	.911	-.083	.122	286.7	1.079	.121	.103
4.5	.910	-.089	.119	297.6	1.042	.097	.089
6.3	.915	-.097	.118	304.7	.935	.086	.093
8.1	.918	-.110	.109	313.9	.896	.058	.094
9.9	.930	-.124	.111	322.7	.869	-.011	.110
11.5	1.019	-.147	.126	328.5	.888	-.049	.107
11.7	.957	-.139	.108	330.2	.883	-.044	.105
13.2	.981	-.153	.108	340.9	.918	-.079	.103
13.6	.984	-.151	.112	345.3	.943	-.076	.106
15.4	1.022	-.158	.114	347.3	.952	-.083	.107
17.1	1.048	-.168	.114	349.2	.949	-.083	.109
18.8	1.070	-.177	.112	350.6	.950	-.084	.110
22.5	1.082	-.181	.106	353.1	.968	-.084	.113
26.1	1.088	-.190	.102	356.9	.950	-.082	.119
29.7	1.091	-.193	.105	357.1	.932	-.087	.119
36.8	1.090	-.198	.118	360.3	.923	-.084	.122
44.1	1.091	-.197	.134				
54.7	1.090	-.206	.156				
62.0	1.099	-.192	.171	ANGLE	VX/V	VT/V	VR/V
72.7	1.100	-.187	.192	1.2	.822	-.011	.024
80.0	1.100	-.166	.201	3.1	.842	-.013	.028
90.8	1.098	-.150	.213	4.8	.843	-.013	.021
99.5	1.097	-.124	.221	6.8	.855	-.015	.023
108.8	1.096	-.105	.223	8.5	.853	-.022	.018
116.0	1.089	-.075	.227	10.5	.865	-.023	.016
126.6	1.086	-.056	.224	12.2	.874	-.035	.013
133.9	1.072	-.035	.224	14.1	.895	-.047	.006
144.7	1.077	.004	.220	16.2	.954	-.068	-.009
152.0	1.066	.028	.228	19.4	.944	-.081	-.025
164.6	1.085	.063	.227	27.3	1.031	-.109	-.006
166.5	1.092	.077	.227	28.5	1.044	-.106	-.006
168.2	1.098	.088	.224	34.1	1.051	-.120	.019
170.0	1.111	.100	.220	46.4	1.074	-.128	.049
173.7	1.126	.120	.205	52.1	1.076	-.127	.069
175.4	1.125	.131	.200	64.5	1.085	-.120	.097
177.3	1.072	.050	.230	70.1	1.085	-.112	.116
179.1	1.041	.029	.223	82.6	1.091	-.090	.132
180.3	1.063	.013	.241	68.1	1.088	-.073	.145
183.0	1.039	.028	.232	100.5	1.090	-.063	.149
184.2	1.069	.050	.238	105.1	1.067	-.034	.155
184.5	1.052	.031	.237	110.7	1.091	-.012	.153
186.5	1.078	.031	.248	124.1	1.092	.006	.158
187.9	1.064	.151	.145	136.7	1.091	.025	.152
190.1	1.053	.146	.158	142.2	1.090	.041	.149
192.0	1.066	.133	.178	147.6	1.094	.068	.159
193.9	1.073	.121	.197	151.3	1.096	.078	.157
196.0	1.088	.113	.223	154.7	1.094	.060	.137
196.7	1.115	.084	.293	154.8	1.098	.090	.158
198.0	1.112	.076	.245	156.5	1.097	.063	.135
199.9	1.111	.068	.244	158.2	1.095	.065	.132
201.3	1.103	.068	.242	158.4	1.098	.095	.156
205.9	1.124	.102	.257	160.2	1.098	.070	.128
214.8	1.103	.124	.245	163.8	1.107	.076	.122
225.6	1.109	.127	.207	165.7	1.117	.078	.120
232.7	1.107	.139	.201	167.6	1.131	.088	.114
241.9	1.111	.145	.183	169.2	1.136	.090	.105
250.7	1.100	.145	.168	169.2	1.135	.084	.108
259.9	1.111	.143	.153	171.0	1.126	.089	.093
268.7	1.098	.140	.136	172.8	1.106	.073	.064

TABLE 5 - CONTINUED

RADIUS = .591			RADIUS = .735				
ANGLE	VX/V	VT/V	VR/V	ANGLE	VX/V		
174.7	1.101	.037	.083	26.1	1.004	-.173	-.014
175.4	1.124	.011	.106	29.7	1.022	-.182	.001
178.1	1.141	-.016	.158	36.8	1.037	-.186	.025
178.2	1.136	.002	.142	44.1	1.042	-.184	.054
180.0	1.150	.006	.165	54.7	1.016	-.181	.079
182.0	1.162	.017	.209	62.0	1.035	-.171	.110
183.7	1.156	.030	.214	72.7	1.050	-.163	.136
185.6	1.140	.042	.212	80.0	1.069	-.146	.158
187.4	1.139	.060	.214	90.8	1.087	-.125	.163
189.0	1.135	.069	.211	99.5	1.099	-.101	.177
192.5	1.117	.093	.209	103.8	1.096	-.085	.174
196.2	1.110	.111	.200	116.0	1.098	-.065	.185
196.2	1.112	.110	.200	126.6	1.094	-.044	.177
199.8	1.112	.125	.191	133.9	1.088	-.029	.181
203.4	1.108	.136	.179	144.7	1.087	-.004	.185
214.2	1.097	.162	.146	152.0	1.078	.003	.186
221.4	1.099	.174	.128	164.6	1.091	.018	.171
232.2	1.093	.185	.106	166.5	1.100	.015	.166
239.4	1.093	.189	.091	168.2	1.105	.013	.157
250.1	1.088	.193	.070	170.0	1.106	.005	.139
257.4	1.083	.193	.055	173.7	1.087	-.060	.115
268.2	1.064	.191	.030	175.4	1.094	-.099	.128
275.5	1.061	.187	.017	177.3	1.048	.191	.049
286.2	1.015	.173	-.006	179.1	1.002	.182	.091
293.4	.985	.159	-.016	180.3	1.014	.182	.025
304.2	.905	.132	-.022	183.0	1.005	.115	.212
311.4	.834	.085	-.023	184.2	1.089	.067	.262
315.1	.797	.052	-.023	184.5	1.056	.068	.274
318.7	.789	.034	-.019	186.5	1.105	.060	.290
322.3	.788	.006	-.017	187.9	1.135	.017	.185
322.3	.800	.009	-.019	190.1	1.135	.036	.179
326.0	.792	-.007	-.012	192.0	1.131	.049	.175
329.7	.792	-.011	-.006	193.9	1.128	.057	.172
333.5	.792	-.019	-.006	196.0	1.132	.065	.172
340.9	.806	-.023	.018	196.7	1.120	.096	.174
342.8	.805	-.021	.022	198.0	1.115	.076	.166
344.7	.788	-.027	.022	199.9	1.114	.082	.200
346.6	.791	-.022	.024	201.3	1.113	.084	.195
348.7	.803	-.022	.027	205.9	1.126	.089	.162
350.5	.809	-.018	.030	214.8	1.108	.117	.141
352.4	.806	-.021	.037	225.6	1.110	.112	.128
356.4	.824	-.018	.031	232.7	1.104	.121	.111
359.7	.831	-.012	.033	241.9	1.102	.124	.099
				250.7	1.086	.127	.080
RADIUS = .735							
ANGLE	VX/V	VT/V	VR/V	ANGLE	VX/V		
.3	.681	-.013	.042	259.9	1.092	.130	.066
2.6	.691	-.020	.029	268.7	1.056	.134	.042
4.3	.736	-.031	.030	277.9	1.041	.128	.031
4.5	.707	-.029	.023	281.4	1.014	.127	.020
6.3	.724	-.032	.007	286.7	.988	.123	.011
8.1	.734	-.046	-.002	297.6	.933	.106	-.010
9.9	.765	-.066	-.012	304.7	.871	.091	-.025
11.5	.874	-.085	-.008	313.9	.790	.054	-.046
11.7	.795	-.081	-.023	322.7	.741	-.006	-.035
13.2	.819	-.097	-.036	330.2	.733	-.018	-.000
13.6	.825	-.108	-.028	340.9	.703	-.036	.052
15.4	.878	-.124	-.033	345.3	.697	-.038	.055
17.1	.915	-.136	-.040	347.1	.685	-.033	.058
18.8	.971	-.149	-.041	347.3	.696	-.032	.068
22.5	.982	-.161	-.034	349.2	.683	-.032	.068
				349.9	.673	-.026	.066
				350.6	.689	-.028	.063

TABLE 5 - CONTINUED

ANGLE	RADIUS = .735			ANGLE	RADIUS = .868		
	VX/V	VT/V	VR/V		VX/V	VT/V	VR/V
353.1	.671	-.026	.068	199.8	1.155	.140	.141
356.9	.674	-.015	.064	203.4	1.155	.139	.128
357.1	.688	-.016	.053	214.2	1.140	.145	.104
360.3	.681	-.013	.042	221.4	1.142	.149	.090
				232.2	1.126	.155	.074
				239.4	1.124	.157	.064
ANGLE	RADIUS = .868			250.1	1.107	.163	.051
	VX/V	VT/V	VR/V	257.4	1.099	.165	.037
-.2	.525	.018	.006	268.2	1.056	.173	.016
1.2	.535	-.012	-.007	275.5	1.037	.170	.011
3.1	.556	-.039	-.017	286.2	.945	.162	-.012
4.8	.566	-.066	-.033	293.4	.906	.157	-.024
6.8	.586	-.091	-.048	304.2	.832	.151	-.041
8.5	.626	-.137	-.062	311.4	.791	.146	-.069
10.5	.686	-.157	-.074	315.1	.748	.146	-.080
12.2	.745	-.168	-.087	318.7	.695	.115	-.087
14.1	.801	-.176	-.097	322.3	.666	.096	-.078
16.2	.869	-.159	-.091	322.3	.662	.087	-.075
19.4	.854	-.167	-.091	326.0	.645	.064	-.057
27.3	.944	-.153	-.027	329.7	.631	.047	-.042
28.5	.959	-.151	-.040	333.5	.633	.036	-.019
34.1	1.003	-.144	-.002	337.2	.612	.045	.009
46.4	1.022	-.122	.030	340.9	.620	.037	.021
52.1	.994	-.103	.057	341.0	.622	.041	.026
64.5	1.035	-.102	.077	342.8	.612	.033	.027
70.1	1.054	-.091	.101	344.7	.596	.047	.044
82.6	1.098	-.090	.119	346.6	.588	.042	.060
88.1	1.127	-.072	.136	348.7	.573	.038	.081
100.5	1.136	-.055	.135	350.5	.560	.038	.083
106.1	1.137	-.037	.146	352.4	.544	.040	.080
118.7	1.148	-.021	.141	356.4	.534	.055	.054
124.1	1.150	-.006	.144	358.1	.523	.032	.018
136.7	1.152	.012	.146	359.7	.532	.024	.010
142.2	1.150	.028	.139	359.8	.525	.018	.006
147.6	1.158	.038	.147				
151.3	1.159	.045	.150				
154.7	1.158	.050	.145				
154.8	1.160	.054	.152				
156.5	1.160	.056	.142				
158.2	1.158	.062	.140				
158.4	1.157	.059	.152				
162.0	1.149	.068	.151				
163.8	1.147	.095	.147				
165.7	1.145	.104	.152				
167.6	1.147	.119	.157				
169.2	1.144	.130	.163				
169.2	1.142	.129	.166				
171.0	1.147	.149	.162				
172.8	1.148	.175	.157				
174.7	1.134	.195	.130				
176.4	1.066	.172	.057				
178.1	1.027	.114	.028				
178.2	1.023	.109	.024				
180.0	1.082	.085	.102				
182.0	1.139	.123	.155				
183.7	1.168	.155	.174				
185.6	1.169	.166	.178				
187.4	1.168	.168	.186				
189.0	1.177	.157	.174				
192.5	1.160	.148	.160				
196.2	1.153	.143	.150				
196.2	1.153	.143	.150				

TABLE 6 - LISTING OF THE MEAN VELOCITY COMPONENT RATIOS, THE MEAN ADVANCE ANGLES AND OTHER DERIVED QUANTITIES AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITHOUT PROPELLER, WITH NOZZLE

					ARS WAKE SURVEY WITH NOZZLE. WITHOUT PROPELLER PROPELLER DIAMETER = 10.50 FEET		JV = .932						
RADIUS	= .451	.591	.735	.868	.299	.300	.400	.500	.600	.700	.800	.900	1.000
VXBAR	= 1.057	1.027	1.001	.996	1.095	1.095	1.069	1.046	1.024	1.005	.996	.996	.996
VTBAR	= -.013	.037	-.007	.042	-.171	-.169	-.054	.015	.031	-.005	.006	.042	.042
VRBAR	= .169	.081	.092	.061	.374	.373	.225	.127	.083	.094	.082	.061	.061
1-WVX	= 1.072	1.055	1.037	1.024	0.000	1.095	1.081	1.068	1.054	1.041	1.030	1.022	1.016
1-WX	= 1.201	1.099	1.059	1.038	0.000	1.392	1.219	1.137	1.090	1.063	1.047	1.033	1.022
BBAR	= 35.03	26.83	22.05	18.54	52.61	52.45	39.55	31.59	26.51	23.12	20.23	17.94	16.26
BPOS	= 4.63	3.26	2.78	3.11	16.50	16.41	7.32	4.05	3.18	2.87	2.93	3.00	2.70
THETA	= 55.00	62.50	97.50	95.00	20.00	20.00	20.00	57.50	62.50	175.00	95.00	95.00	95.00
BNEG	= -5.56	-5.61	-6.72	-8.50	-23.94	-23.68	-5.71	-5.61	-5.54	-6.21	-7.57	-8.24	-7.51
THETA	= 317.50	317.50	355.00	357.50	180.00	180.00	190.00	317.50	317.50	355.00	355.00	357.50	0.00

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VXBAR IS CIRCUMFERENTIAL MEAN LONGITUDINAL VELOCITY.

VTBAR IS CIRCUMFERENTIAL MEAN TANGENTIAL VELOCITY.

VRBAR IS CIRCUMFERENTIAL MEAN RADIAL VELOCITY.

1-WVX IS VOLUMETRIC MEAN WAKE VELOCITY WITHOUT TANGENTIAL CORRECTION.

1-WX IS VOLUMETRIC MEAN WAKE VELOCITY WITH TANGENTIAL CORRECTION.

BBAR IS MEAN ANGLE OF ADVANCE.

BPOS IS VARIATION BETWEEN THE MAXIMUM AND MEAN ADVANCE ANGLES (DELTA BETA PLUS).

BNEG IS VARIATION BETWEEN THE MINIMUM AND MEAN ADVANCE ANGLES (DELTA BETA MINUS).

THETA IS ANGLE IN DEGREES AT WHICH CORRESPONDING BPOS OR BNEG OCCURS.

TABLE 7 - HARMONIC ANALYSIS OF THE LONGITUDINAL VELOCITY COMPONENT RATIOS AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITHOUT PROPELLER, WITH NOZZLE

ARS WAKE SURVEY WITH NOZZLE, WITHOUT PROPELLER PROPELLER DIAMETER = 10.50 FEET JV = .932									
HARMONIC ANALYSES OF LONGITUDINAL VELOCITY COMPONENT RATIOS (VX/V)									
HARMONIC	=	1	2	3	4	5	6	7	8
RADIUS = .451									
AMPLITUDE =	.0647	.0633	.0287	.0158	.0049	.0118	.0089	.0158	
PHASE ANGLE =	290.0	318.7	346.1	16.3	92.8	195.6	221.3	222.5	
RADIUS = .591									
AMPLITUDE =	.1289	.0700	.0413	.0129	.0063	.0074	.0121	.0050	
PHASE ANGLE =	290.3	320.2	327.7	17.3	232.4	189.9	231.7	228.9	
RADIUS = .735									
AMPLITUDE =	.1576	.0998	.0425	.0301	.0137	.0187	.0112	.0133	
PHASE ANGLE =	286.0	311.5	334.6	335.1	289.1	266.9	239.2	249.7	
RADIUS = .868									
AMPLITUDE =	.2355	.1166	.0504	.0330	.0220	.0245	.0129	.0117	
PHASE ANGLE =	286.3	304.5	326.5	319.1	290.8	274.3	228.0	242.8	
RADIUS = .299									
AMPLITUDE =	.0480	.0636	.0348	.0398	.0246	.0296	.0036	.0476	
PHASE ANGLE =	127.4	300.2	62.1	342.2	47.2	242.7	147.7	228.2	
RADIUS = .300									
AMPLITUDE =	.0471	.0635	.0346	.0395	.0244	.0294	.0036	.0473	
PHASE ANGLE =	127.5	300.3	61.8	342.4	47.3	242.5	148.8	228.2	
RADIUS = .400									
AMPLITUDE =	.0325	.0612	.0247	.0205	.0099	.0150	.0063	.0241	
PHASE ANGLE =	284.4	314.3	7.7	2.4	66.5	214.5	212.7	224.8	
RADIUS = .500									
AMPLITUDE =	.0913	.0657	.0339	.0136	.0031	.0102	.0105	.0101	
PHASE ANGLE =	291.0	320.8	335.0	26.0	156.7	182.2	226.1	220.5	
RADIUS = .600									
AMPLITUDE =	.1289	.0777	.0411	.0140	.0063	.0073	.0120	.0057	
PHASE ANGLE =	289.9	319.6	328.6	10.7	239.9	201.7	232.7	234.0	
RADIUS = .700									
AMPLITUDE =	.1452	.0946	.0415	.0270	.0114	.0157	.0112	.0122	
PHASE ANGLE =	286.5	313.4	334.6	339.9	284.8	261.9	239.3	249.2	
RADIUS = .800									
AMPLITUDE =	.1895	.1096	.0454	.0333	.0179	.0228	.0117	.0136	
PHASE ANGLE =	285.8	308.0	332.0	327.7	291.7	271.8	235.5	246.4	
RADIUS = .900									
AMPLITUDE =	.2355	.1166	.0504	.0330	.0220	.0245	.0129	.0117	
PHASE ANGLE =	286.3	304.5	326.5	319.1	290.8	274.3	228.0	242.8	
RADIUS = 1.000									
AMPLITUDE =	.2355	.1166	.0504	.0330	.0220	.0245	.0129	.0117	
PHASE ANGLE =	286.3	304.5	326.5	319.1	290.8	274.3	228.0	242.8	

TABLE 8 - HARMONIC ANALYSIS OF THE TANGENTIAL VELOCITY COMPONENT RATIOS AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITHOUT PROPELLER, WITH NOZZLE

ARS WAKE SURVEY WITH NOZZLE, WITHOUT PROPELLER PROPELLER DIAMETER = 10.50 FEET JV = .932									
HARMONIC ANALYSES OF TANGENTIAL VELOCITY COMPONENT RATIOS (VT/V)									
HARMONIC	=	1	2	3	4	5	6	7	8
RADIUS = .451									
AMPLITUDE =	.1709	.0220	.0075	.0051	.0087	.0076	.0066	.0044	
PHASE ANGLE =	214.3	197.1	346.8	79.4	36.4	98.8	78.1	127.6	
RADIUS = .591									
AMPLITUDE =	.1455	.0246	.0211	.0074	.0211	.0022	.0116	.0039	
PHASE ANGLE =	210.4	243.3	50.0	10.4	66.0	152.1	85.3	243.5	
RADIUS = .735									
AMPLITUDE =	.1473	.0225	.0090	.0121	.0128	.0116	.0065	.0083	
PHASE ANGLE =	207.7	193.9	94.0	62.7	87.0	86.2	100.6	83.2	
RADIUS = .868									
AMPLITUDE =	.1507	.0322	.0220	.0127	.0092	.0163	.0083	.0131	
PHASE ANGLE =	210.6	190.0	224.1	142.3	176.3	122.2	126.4	128.4	
RADIUS = .299									
AMPLITUDE =	.2295	.0713	.0534	.0276	.0335	.0335	.0104	.0317	
PHASE ANGLE =	217.8	140.1	245.8	122.6	261.0	84.2	269.6	93.3	
RADIUS = .300									
AMPLITUDE =	.2290	.0707	.0529	.0273	.0332	.0333	.0102	.0315	
PHASE ANGLE =	217.8	140.2	245.9	122.5	261.1	84.3	269.7	93.4	
RADIUS = .400									
AMPLITUDE =	.1870	.0305	.0143	.0100	.0065	.0140	.0024	.0109	
PHASE ANGLE =	215.6	166.9	270.3	109.4	309.0	90.3	62.6	104.0	
RADIUS = .500									
AMPLITUDE =	.1589	.0217	.0138	.0046	.0151	.0038	.0095	.0028	
PHASE ANGLE =	212.9	225.4	32.0	29.2	55.3	118.2	81.5	201.7	
RADIUS = .600									
AMPLITUDE =	.1455	.0236	.0207	.0080	.0208	.0023	.0111	.0028	
PHASE ANGLE =	210.1	240.1	52.0	16.9	66.8	125.1	85.5	244.3	
RADIUS = .700									
AMPLITUDE =	.1467	.0207	.0129	.0122	.0153	.0099	.0072	.0065	
PHASE ANGLE =	207.8	202.1	76.4	52.5	79.3	82.1	94.0	76.4	
RADIUS = .800									
AMPLITUDE =	.1408	.0269	.0078	.0107	.0085	.0138	.0066	.0105	
PHASE ANGLE =	208.5	187.7	185.5	92.0	116.0	100.1	115.4	101.5	
RADIUS = .900									
AMPLITUDE =	.1507	.0322	.0220	.0127	.0092	.0163	.0083	.0131	
PHASE ANGLE =	210.6	190.0	224.1	142.3	176.3	122.2	126.4	128.4	
RADIUS = 1.000									
AMPLITUDE =	.1507	.0322	.0220	.0127	.0092	.0163	.0083	.0131	
PHASE ANGLE =	210.6	190.0	224.1	142.3	176.3	122.2	126.4	128.4	

TABLE 9 - EXPERIMENTAL WAKE SURVEY DATA FOR THE ARS-50 WITHOUT NOZZLE OR PROPELLER

ANGLE	RADIUS = .451	VX/V	VT/V	VR/V	ANGLE	RADIUS = .591	VX/V	VT/V	VR/V
-.8	.887	-.091	.090		-1.6	.837	-.016	-.004	
7.4	.909	-.130	.099		5.7	.852	-.022	-.008	
16.4	1.018	-.187	.097		16.4	.933	-.089	-.049	
25.4	1.059	-.209	.084		23.7	1.019	-.112	-.044	
34.4	1.051	-.219	.094		34.4	1.021	-.137	-.017	
43.4	1.055	-.229	.114		41.5	1.030	-.150	.004	
52.4	1.054	-.236	.136		52.4	1.027	-.159	.042	
61.3	1.055	-.233	.158		59.5	1.041	-.155	.068	
70.4	1.051	-.222	.177		70.4	1.031	-.142	.105	
79.5	1.048	-.205	.194		77.6	1.023	-.127	.121	
88.4	1.047	-.183	.208		88.3	1.029	-.097	.145	
98.1	1.047	-.160	.218		95.7	1.020	-.079	.150	
106.4	1.031	-.130	.225		106.3	1.016	-.045	.163	
115.5	1.035	-.093	.229		113.7	1.012	-.026	.165	
133.5	1.031	-.030	.229		124.4	1.002	.009	.169	
151.5	1.039	.025	.227		131.9	1.005	.028	.169	
160.5	1.021	.063	.220		142.5	1.006	.060	.169	
169.5	1.042	.101	.215		149.9	1.013	.085	.166	
178.4	1.013	.156	.172		150.6	1.012	.080	.167	
187.5	.979	.171	.133		155.3	1.011	.101	.164	
196.5	1.004	.139	.216		160.7	1.005	.120	.161	
205.6	1.055	.148	.274		168.0	1.002	.157	.155	
214.5	1.058	.165	.255		169.5	1.007	.169	.156	
223.5	1.053	.177	.218		178.7	.960	.195	.110	
232.6	1.058	.188	.196		179.7	.982	.204	.116	
241.4	1.051	.190	.173		185.8	.938	.151	.116	
251.0	1.057	.191	.166		196.7	1.020	.192	.164	
259.5	1.059	.183	.135		203.8	1.025	.221	.164	
270.2	1.057	.180	.118		214.6	1.024	.231	.142	
277.5	1.061	.163	.098		221.7	1.027	.234	.124	
286.6	1.053	.147	.084		232.6	1.028	.243	.090	
295.6	1.041	.125	.072		239.7	1.024	.247	.071	
304.6	.986	.105	.071		250.5	1.020	.247	.043	
313.7	.844	.078	.073		257.8	1.023	.243	.023	
322.8	.782	.011	.076		268.5	1.004	.236	-.007	
331.8	.845	-.045	.074		275.8	1.006	.226	-.024	
340.9	.269	-.073	.076		293.7	.942	.191	-.063	
350.1	.894	-.085	.042		304.5	.870	.157	-.063	
356.0	.863	-.089	.067		311.7	.806	.114	-.058	
359.2	.887	-.091	.090		322.5	.766	.024	-.040	
					329.6	.785	-.001	-.037	
					340.5	.739	-.016	-.026	
					347.6	.809	-.015	-.007	
					356.0	.831	-.016	-.005	
					358.4	.837	-.016	-.004	

TABLE 9 - CONTINUED

ANGLE	RADIUS = .735			RADIUS = .868		
	VX/V	VT/V	VR/V	ANGLE	VX/V	VT/V
-1.6	.710	-.036	.019	-1.6	.588	.033
7.4	.730	-.038	-.023	0.0	.582	.026
16.4	.855	-.109	-.086	5.7	.562	.003
25.4	.959	-.173	-.079	16.4	.821	-.125
34.4	.982	-.206	-.034	23.7	.904	-.146
43.4	.980	-.220	.001	34.4	.946	-.165
52.4	.956	-.222	.042	41.5	.932	-.167
61.3	.960	-.219	.081	52.4	.894	-.157
70.4	.968	-.205	.116	59.5	.912	-.146
79.5	.981	-.185	.142	70.4	.943	-.141
88.4	.989	-.159	.162	77.6	.969	-.128
98.1	.997	-.133	.171	88.3	.988	-.097
106.4	.995	-.108	.179	95.7	.987	-.078
115.5	.996	-.076	.185	106.3	.988	-.049
133.5	.998	-.030	.190	113.7	.989	-.032
151.5	.997	.016	.189	124.4	.988	-.006
160.5	.967	.050	.184	131.9	.991	.010
169.5	.999	.079	.172	142.5	.985	.035
178.4	.865	.087	.097	149.9	.993	.059
187.5	1.003	.059	.190	155.3	.993	.071
196.5	1.000	.107	.168	161.2	.994	.087
205.6	1.009	.123	.160	169.5	.960	.146
214.5	1.004	.140	.140	178.7	.684	.026
223.5	1.015	.152	.123	179.7	.629	.058
232.6	1.009	.160	.100	185.8	.999	.112
241.4	1.006	.166	.083	190.0	.996	.124
251.0	1.011	.166	.057	196.7	.992	.143
259.5	1.003	.165	.037	203.8	.991	.166
270.2	1.006	.160	.010	214.6	.996	.184
277.5	.981	.154	-.009	221.7	1.005	.195
286.6	.946	.139	-.027	232.6	1.001	.205
295.6	.902	.122	-.052	239.7	1.005	.212
304.6	.843	.097	-.065	250.5	.998	.216
313.7	.734	.053	-.075	257.8	.996	.215
322.8	.719	-.002	-.060	268.5	.969	.214
331.8	.712	-.012	-.032	275.8	.952	.200
340.9	.682	-.019	-.001	293.7	.858	.173
350.1	.649	-.035	.014	304.5	.783	.154
356.0	.692	-.036	.018	311.7	.712	.135
358.4	.710	-.036	.019	322.5	.638	.054
				329.6	.626	.054
				340.5	.627	.068
				347.6	.589	.046
				355.0	.588	.034
				358.4	.588	.033
				360.0	.582	.026
						-.016

TABLE 10 - LISTING OF THE MEAN VELOCITY COMPONENT RATIOS, THE MEAN ADVANCE ANGLES AND OTHER DERIVED QUANTITIES AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITHOUT NOZZLE OR PROPELLER

ARS WAKE SURVEY WITHOUT PROPELLER OR NOZZLE PROPELLER DIAMETER = 10.50 FEET										JV = .9332			
	RADIUS *	.451	.591	.735	.868	.299	.300	.400	.500	.700	.800	.900	1.000
45	VXBAR *	1.009	.970	.928	.891	1.049	1.049	1.023	.996	.968	.938	.910	.891
	VTBAR *	- .003	.061	- .001	.048	- .210	- .209	- .056	.033	.054	.003	.010	.048
	VRBAR *	.156	.063	.071	.037	.369	.367	.214	.112	.065	.074	.060	.037
	1-WVX *	1.025	1.006	.982	.958	0.000	1.049	1.036	1.021	1.005	.988	.970	.954
	1-WX *	1.171	1.051	1.002	.971	0.000	1.393	1.190	1.095	1.041	1.008	.986	.946
	BBAR *	33.63	25.29	20.54	16.68	52.76	52.58	38.37	30.09	24.99	21.65	18.58	14.61
	BPOS *	5.76	4.24	2.97	2.57	10.82	10.76	6.74	5.18	4.12	3.21	2.56	2.18
	THETA *	55.00	60.00	40.00	87.50	32.50	50.00	60.00	60.00	42.50	37.50	37.50	87.50
	BNEG	-6.67	-4.63	-5.67	-5.83	-14.46	-14.37	-8.34	-5.62	-4.63	-5.34	-5.85	-5.16
	THETA	320.00	317.50	350.00	5.00	322.50	322.50	320.00	317.50	347.50	350.00	5.00	5.00

VXBAR IS CIRCUMFERENTIAL MEAN LONGITUDINAL VELOCITY.

VTBAR IS CIRCUMFERENTIAL MEAN TANGENTIAL VELOCITY.

VRBAR IS CIRCUMFERENTIAL MEAN RADIAL VELOCITY.

1-WVX IS VOLUMETRIC MEAN WAKE VELOCITY WITHOUT TANGENTIAL CORRECTION.

1-WX IS VOLUMETRIC MEAN WAKE VELOCITY WITH TANGENTIAL CORRECTION.

BBAR IS MEAN ANGLE OF ADVANCE.

BPOS IS VARIATION BETWEEN THE MAXIMUM AND MEAN ADVANCE ANGLES (DELTA BETA PLUS).

BNEG IS VARIATION BETWEEN THE MINIMUM AND MEAN ADVANCE ANGLES (DELTA BETA MINUS).

THETA IS ANGLE IN DEGREES AT WHICH CORRESPONDING BPOS OR BNEG OCCURS.

TABLE 11 - HARMONIC ANALYSIS OF THE LONGITUDINAL VELOCITY COMPONENT RATIOS AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITHOUT NOZZLE OR PROPELLER

ARS WAKE SURVEY WITHOUT PROPELLER OR NOZZLE PROPELLER DIAMETER = 10.50 FEET JV = .932									
HARMONIC ANALYSES OF LONGITUDINAL VELOCITY COMPONENT RATIOS (VX/V)									
HARMONIC	=	1	2	3	4	5	6	7	8
RADIUS = .451									
AMPLITUDE =	.0543	.0659	.0413	.0196	.0159	.0132	.0099	.0172	
PHASE ANGLE =	293.2	314.6	350.1	1.5	67.2	190.7	212.1	229.0	
RADIUS = .591									
AMPLITUDE =	.0759	.0747	.0362	.0128	.0075	.0124	.0042	.0113	
PHASE ANGLE =	300.3	321.7	353.1	351.3	78.3	225.8	223.2	248.6	
RADIUS = .735									
AMPLITUDE =	.1121	.0905	.0442	.0290	.0040	.0197	.0094	.0115	
PHASE ANGLE =	286.5	309.1	344.9	330.0	308.0	266.7	219.9	263.9	
RADIUS = .868									
AMPLITUDE =	.1394	.1114	.0414	.0361	.0056	.0357	.0146	.0268	
PHASE ANGLE =	286.2	303.8	356.1	314.9	357.6	272.7	192.6	261.5	
RADIUS = .299									
AMPLITUDE =	.0651	.0761	.0621	.0491	.0259	.0143	.0281	.0308	
PHASE ANGLE =	249.4	283.1	340.3	350.9	47.8	179.8	209.4	219.0	
RADIUS = .300									
AMPLITUDE =	.0648	.0759	.0619	.0488	.0258	.0143	.0279	.0307	
PHASE ANGLE =	249.7	283.3	340.3	351.0	47.9	179.8	209.4	219.0	
RADIUS = .400									
AMPLITUDE =	.0512	.0654	.0464	.0268	.0189	.0139	.0146	.0210	
PHASE ANGLE =	280.7	305.9	346.9	357.9	60.9	184.5	210.5	224.5	
RADIUS = .500									
AMPLITUDE =	.0605	.0683	.0381	.0150	.0130	.0126	.0067	.0144	
PHASE ANGLE =	299.6	319.8	352.4	2.9	72.5	199.9	214.9	234.8	
RADIUS = .600									
AMPLITUDE =	.0782	.0754	.0370	.0140	.0065	.0124	.0046	.0108	
PHASE ANGLE =	298.6	320.7	351.7	348.7	76.5	229.3	225.4	249.6	
RADIUS = .700									
AMPLITUDE =	.1037	.0858	.0434	.0259	.0028	.0166	.0063	.0099	
PHASE ANGLE =	288.0	311.4	344.8	333.6	316.3	261.2	224.9	262.0	
RADIUS = .800									
AMPLITUDE =	.1264	.1001	.0439	.0333	.0050	.0268	.0116	.0172	
PHASE ANGLE =	285.5	305.9	348.0	323.1	319.0	271.6	207.4	263.6	
RADIUS = .900									
AMPLITUDE =	.1394	.1114	.0414	.0361	.0056	.0357	.0146	.0268	
PHASE ANGLE =	286.2	303.8	356.1	314.9	357.6	272.7	192.6	261.5	
RADIUS = 1.000									
AMPLITUDE =	.1394	.1114	.0414	.0361	.0056	.0357	.0146	.0268	
PHASE ANGLE =	286.2	303.8	356.1	314.9	357.6	272.7	192.6	261.5	

TABLE 12 - HARMONIC ANALYSIS OF THE TANGENTIAL VELOCITY COMPONENT RATIOS AT THE EXPERIMENTAL AND INTERPOLATED RADII FOR THE ARS-50 WITHOUT NOZZLE OR PROPELLER

ARS WAKE SURVEY WITHOUT PROPELLER OR NOZZLE PROPELLER DIAMETER = 10.50 FEET									JV = .932	
HARMONIC	=	1	2	3	4	5	6	7	8	(VT/V)
RADIUS = .451										
AMPLITUDE =	.2141	.0199	.0059	.0082	.0036	.0117	.0007	.0091		
PHASE ANGLE =	214.8	175.9	313.6	65.5	333.6	80.4	87.6	100.6		
RADIUS = .591										
AMPLITUDE =	.1965	.0107	.0117	.0143	.0118	.0098	.0051	.0072		
PHASE ANGLE =	215.5	200.4	24.7	52.3	46.5	108.0	70.8	151.5		
RADIUS = .735										
AMPLITUDE =	.1787	.0233	.0175	.0140	.0133	.0083	.0065	.0024		
PHASE ANGLE =	208.7	169.9	70.1	71.1	57.3	101.8	48.6	152.4		
RADIUS = .868										
AMPLITUDE =	.1750	.0281	.0165	.0110	.0135	.0098	.0113	.0050		
PHASE ANGLE =	206.8	190.6	109.7	123.3	94.5	137.3	92.4	179.6		
RADIUS = .299										
AMPLITUDE =	.2345	.0594	.0195	.0131	.0227	.0209	.0083	.0228		
PHASE ANGLE =	207.6	158.9	226.6	176.0	248.0	46.3	264.6	54.6		
RADIUS = .300										
AMPLITUDE =	.2343	.0591	.0194	.0129	.0225	.0208	.0082	.0226		
PHASE ANGLE =	207.7	159.0	226.9	175.7	248.1	46.5	264.6	54.8		
RADIUS = .400										
AMPLITUDE =	.2205	.0296	.0083	.0056	.0072	.0137	.0018	.0120		
PHASE ANGLE =	213.0	167.4	270.1	99.2	270.6	67.1	258.6	79.5		
RADIUS = .500										
AMPLITUDE =	.2080	.0141	.0062	.0110	.0063	.0107	.0027	.0079		
PHASE ANGLE =	215.7	187.4	348.2	55.0	26.3	92.6	79.0	122.8		
RADIUS = .600										
AMPLITUDE =	.1949	.0114	.0122	.0146	.0120	.0097	.0051	.0067		
PHASE ANGLE =	215.0	193.7	29.6	53.2	46.5	106.4	65.7	150.9		
RADIUS = .700										
AMPLITUDE =	.1816	.0209	.0168	.0147	.0133	.0085	.0061	.0029		
PHASE ANGLE =	209.9	169.3	62.2	64.9	52.8	99.0	43.6	147.4		
RADIUS = .800										
AMPLITUDE =	.1756	.0261	.0175	.0119	.0130	.0082	.0078	.0028		
PHASE ANGLE =	207.1	176.6	86.1	89.3	72.2	115.7	68.7	170.5		
RADIUS = .900										
AMPLITUDE =	.1750	.0281	.0165	.0110	.0135	.0098	.0113	.0050		
PHASE ANGLE =	206.8	190.6	103.7	123.3	94.5	137.3	92.4	179.6		
RADIUS = 1.000										
AMPLITUDE =	.1750	.0281	.0165	.0110	.0135	.0098	.0113	.0050		
PHASE ANGLE =	206.8	190.6	109.7	123.3	94.5	137.3	92.4	179.6		

**DTNSRDC ISSUES THREE TYPES OF REPORTS**

- 1. DTNSRDC REPORTS, A FORMAL SERIES, CONTAIN INFORMATION OF PERMANENT TECHNICAL VALUE. THEY CARRY A CONSECUTIVE NUMERICAL IDENTIFICATION REGARDLESS OF THEIR CLASSIFICATION OR THE ORIGINATING DEPARTMENT.**
- 2. DEPARTMENTAL REPORTS, A SEMIFORMAL SERIES, CONTAIN INFORMATION OF A PRELIMINARY, TEMPORARY, OR PROPRIETARY NATURE OR OF LIMITED INTEREST OR SIGNIFICANCE. THEY CARRY A DEPARTMENTAL ALPHANUMERICAL IDENTIFICATION.**
- 3. TECHNICAL MEMORANDA, AN INFORMAL SERIES, CONTAIN TECHNICAL DOCUMENTATION OF LIMITED USE AND INTEREST. THEY ARE PRIMARILY WORKING PAPERS INTENDED FOR INTERNAL USE. THEY CARRY AN IDENTIFYING NUMBER WHICH INDICATES THEIR TYPE AND THE NUMERICAL CODE OF THE ORIGINATING DEPARTMENT. ANY DISTRIBUTION OUTSIDE DTNSRDC MUST BE APPROVED BY THE HEAD OF THE ORIGINATING DEPARTMENT ON A CASE-BY-CASE BASIS.**

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